

Chemical kinetics.

It is a branch of physical chemistry. It deals with the rate of reaction is called the "chemical kinetics".

The study of chemical kinetics used to know the followings:

- i) The rate of reaction and rate laws.
- ii) The factors temperature, pressure, concentration and catalyst influence.

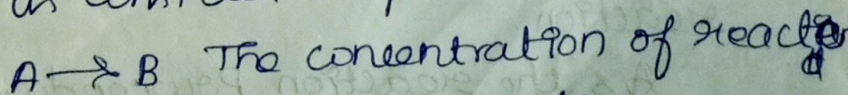
The Mechanism or the sequence of the steps by which a reaction occurs.

The knowledge of the rate of reactions is very valuable to understand the chemical of reactions. It is also great importance in selecting optimum conditions for an industrial process to proceed as maximum yield.

Reaction Rate:

The rate of reaction tell us to what speed reaction occurs.

Let us consider simple reaction



A decreases and B increases as time passes.

$$\text{rate} = -\frac{d[A]}{dt} \quad (\text{or}) \quad \text{rate} = +\frac{d[B]}{dt}$$

d → infinitesimally small concentration in moles per litre.

It is defined as the change in concentration of any of reactant (or) products per unit time.

For a given reaction, the rate of reaction may be equal to the rate of disappearance of A is equal to the rate of appearance of B.

The negative sign shows the concentration of the reactant A decreases, The positive sign indicates the increasing concentration of B.

UNIT

Rate
Units of concentration:

The Reaction rate has unit of concentrations divide by time.

mole / litre sec (or) $\text{mol l}^{-1} \text{s}^{-1}$

mole / litre min (or) $\text{mol l}^{-1} \text{min}^{-1}$

mole / litre hour (or) $\text{mol l}^{-1} \text{h}^{-1}$ and so on.

They are two type of rate of reaction measured for chemical reaction.

i) Average Rate of Reaction

ii) Instantaneous Rate of Reaction

i) Average rate of reaction:

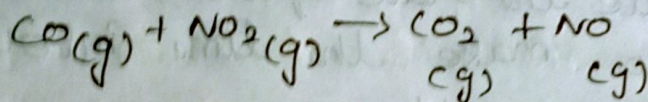
These depends on chemical and Nature of reaction.

As the reaction proceeds, the concentration of reactant A

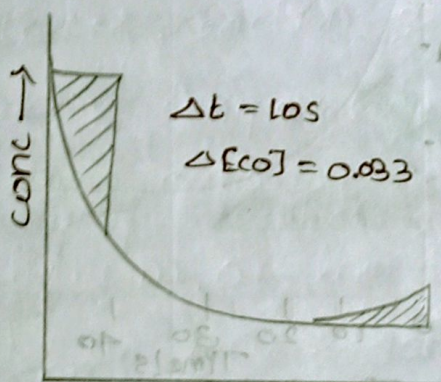
Conc of CO:

0.100 0.067 0.050 0.040 0.033
 (0) (10) (20) (30) (40)

Time seconds



$$\text{rate} = -\frac{\Delta[\text{CO}]}{\Delta t} = -\frac{d[\text{CO}]}{dt}$$



0.067
 0.100
 3.916
 0.100
 0.667
 0.033
 Δt = 10s
 Δ[CO] = 0.033

time → fig-1

over the 10sec average rate,

$$-\frac{d[\text{CO}]}{dt} = \frac{-(0.067 - 0.100)}{(10 - 0)} = \frac{0.033}{10} = 0.0033 \text{ mol l}^{-1} \text{ s}^{-1}$$

The results are shown in graphically in figure 1.

As a reaction proceeds, where conc. of CO decreases rapidly the initial stage of reaction. Then the conc. of CO decreases more and more slowly. The rate of reaction is a function of time. The reaction is slowing down with time. As indicated the experimental data.

The Average rate are not always useful because they cover a large time interval during which the rate of reaction changes significantly. So the better way to estimate the rate of the reaction, we need to make the time interval as small as possible.

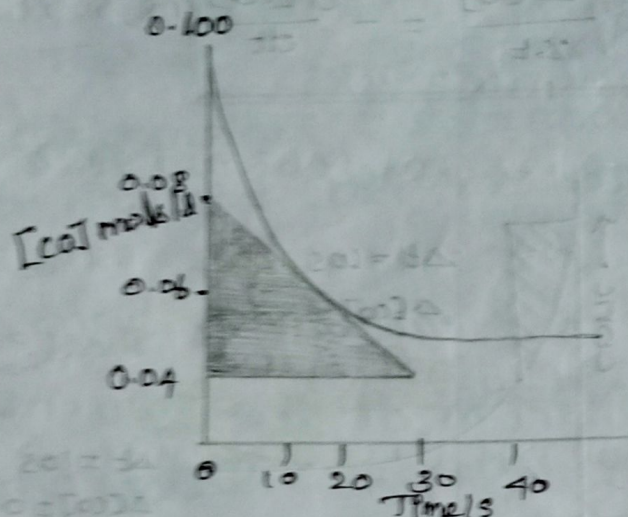


Fig: 2

The slope of tangent at 10s is equal to the instantaneous rate.

Instantaneous Rate of reaction:

The Average rates not useful, the better way to estimate the rate of reaction is to make the time interval as small as possible. If the time interval is infinitesimally small (very very small) (Δt approaches to 0), The rate is referred to as the 'instantaneous rate' and is written calculus as equation(1)

$$\text{rate} = \frac{d[\text{J}]_t}{dt} \rightarrow \text{①}$$

$$\text{Instantaneous rate} = -\frac{d[\text{CO}]}{dt} \rightarrow \text{②}$$

where $[\text{J}]_t$ is conc. at time t .

Conc \rightarrow concentration
Therefore, The Instantaneous rate at any time is equal to the slope of a straight line drawn of tangent curve at a time.

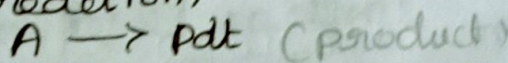
for example, In figure 2. The Instantaneous rate at 105 s is found to be $0.0022 \text{ mol/l/sec}^{-1}$

Rate Laws (or) Rate equation

At a fixed temperature, the rate of a given reaction depends on conc. of reactants. To the relation between conc. and rate is determined by measuring the reaction rate with different initial reactant conc.

By a study of numerous reactions, it is shown that: The rate of a reaction directly proportional to reactant conc., each conc. is raised to some power.

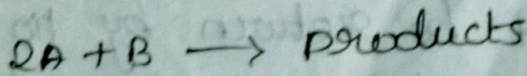
For a substance A under go reaction
For a reaction,



$$\text{rate} \propto [A]^n$$

$$\text{(or)} \quad \text{rate} = k [A]^n \quad \text{--- (1)}$$

For a reaction:



$$\text{rate} = k [A]^m [B]^n \quad \text{--- (2)}$$

The rate of a reaction may be expressed as eqn (1) and (2). indicates, the relation between the rate of a reaction and reactant [].

An equation which shows how the reaction rate is related to concentration is called "rate law con rate equation".

order of a reaction:

Reaction	Rate law (rate = $k[A]^m[B]^n$)	Reaction order m+n
① $2N_2O_5 \rightarrow 4NO_2 + O_2$	rate = $k[N_2O_5]$	1 (First order)
② $H_2 + I_2 \rightarrow 2HI$	rate = $k[H_2][I_2]$	1+1=2 (Second)
③ $2NO_2 \rightarrow 2NO + O_2$	rate = $k[NO_2]^2$	2
④ $2NO + 2H_2 \rightarrow N_2 + 2H_2O$	rate = $k[H_2][NO]^2$	1+2=3 (Third order)
⑤ $NO_2 + CO \rightarrow NO + CO_2$	rate = $k[NO_2]^2 [CO]^0$	2+0 (second and 0 (zero) 0)

The rate law for a reaction must be determined ~~it can't be~~ by experiment

It can't be given by the equation with knowledge of law of mass action.

However, for some elementary reaction

The powers in the rate law may correspond to co-efficient in the chemical equation. But usually the powers of concentration in the rate law are different from co-efficient.

"The order of reaction depends on the sum of the powers of concentration in the rate law."

Let us consider the example of reaction for the rate law.

$$\text{rate} = k[A]^m[B]^n$$

The order of such a reaction (m+n)
The order of reaction also be defined to a single reactant.

Thus the reaction order with respect to A is m and with respect to B is n.

The overall order of reaction (m+n) have range from 1 to 3 and can be fractional

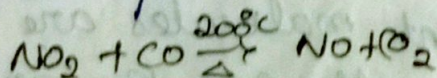
Zero order reaction:

Def:

The Zero order reaction is one whose rate is independent of concentration and does not affect the reaction rate, not include in the rate law.

Such reactant power 0 (zero)

The example,



$$\text{rate} = k[\text{NO}_2]^0[\text{CO}]^0$$

respect to $\text{[NO}_2\text{]}$. The overall

molecularity of reaction:

Chemical reaction classified into
types:

1) Elementary reaction

2) Complex reaction

Elementary reaction:-

Elementary reaction is a simple
reaction which occurs in a single step

A complex reaction is occurs
two or more steps

Molecularity of elementary reactions:

It is defined as the number of
reactant molecules involved in a reaction

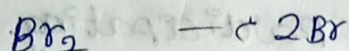
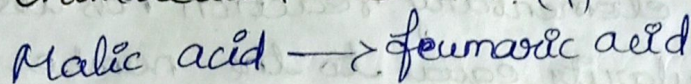
The molecularity of an elementary
reaction is one, 2, 3... etc. according to

1) 3 reactant molecules are
participating in the reaction are

called unimolecular, bimolecular and
termolecular reaction respectively.

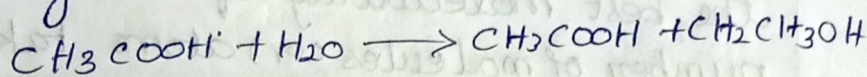
Ex:

a) Unimolecular reaction: (1)

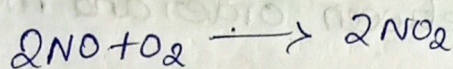


Bimolecular reaction: (2)

Ethyl acetate + water



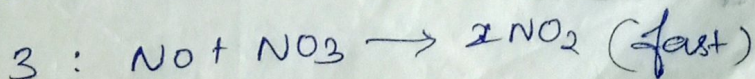
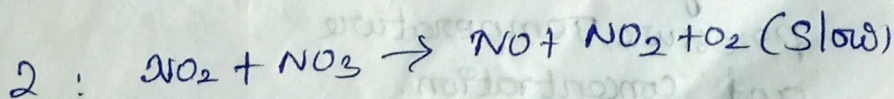
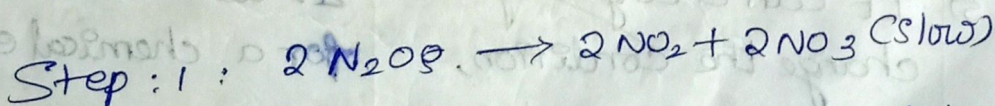
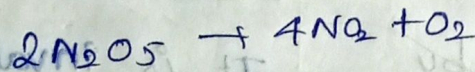
Ter molecular reaction: (3)



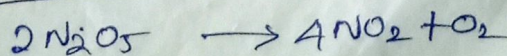
Molecularity of a complex reaction:

Most of the reactions are complex reactions occur in a series of steps. Each step is an elementary reaction. Thus step wise sequence of elementary reactions is called the mechanism of the reaction. here sum of step will be fast others will be slow. Thus the slowest step is a rate determining step of the reaction.

Ex:



Overall
reaction



A

Each elementary reaction has its own molecularity equal to the number of molecules or atoms participating.

The molecularity of the overall reaction is different with different steps, ~~it is~~ the best molecularity of reaction is the number of molecules (or) atoms taking part in the rate determining step.

✓ Difference between order and molecularity.

Order of a Reaction:

- 1) It is the sum of powers of the concentration terms in the rate law equation.
- 2) Experimentally determined value
- 3) It can have fractional values.
- 4) It can assume zero value.
- 5) It can change by change the condition, pressure, temperature and concentration.

Molecularity of Reaction:

- It is the number of reacting species under going simultaneous collision in the simple reaction.
- It is a theoretical concept.
- It is always whole number val.
- It can't have zero value.
- It is invariant for a chemical equation.

✓ Derivation of rate constant of a zero order reaction:-

rate is independent of the reactions.

ex: photoelectric reaction
 $A \rightarrow \text{products}$

Initial conc. a 0

final conc. $a-x$ x

$$\text{Rate of reaction} = -\frac{d[A]}{dt} = k_0[A]^0$$

(or)

$$\frac{dx}{dt} = \frac{-d(a-x)}{dt}$$

conc. of reaction

$$= k_0(a-x)^0$$

$$\frac{dx}{dt} = k_0$$

on integration we get

$$\int dx = k_0 \int dt$$

$$x = k_0 t$$

$$\frac{x}{t} = k_0$$

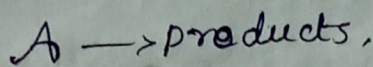
rate constant = k

is equal to all conc. of reaction.

When k_0 is a rate constant of a zero order reaction, the unit is the conc. per unit time. In zero order reaction the rate constant is equal to the rate of reaction at all concentrations.

✓ Derivation of rate constant of a first order reactions:

Let us consider the first order reactions



$$-\frac{dx}{dt} = k(a-x)$$

(or)

$$\frac{dx}{(a-x)} = k dt \rightarrow \textcircled{1}$$

Integration of the eqn $\textcircled{1}$, we get

$$-\int \frac{dx}{a-x} = \int k dt$$

$$-\ln(a-x) = kt + I$$

The constant k evaluated by putting $t=0, x=0,$

$$\text{Then } I = -\ln a$$

Sub. for I in eqn $\textcircled{2}$

$$-\ln(a-x) = kt - \ln a$$

$$\ln a - \ln(a-x) = kt$$

$$\ln \left(\frac{a}{a-x} \right) = kt \rightarrow \textcircled{3}$$

$$\text{(or)} \quad k = \frac{1}{t} \ln \left(\frac{a}{a-x} \right)$$

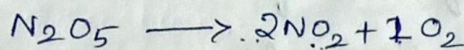
change \ln to common \log

$$k = \frac{2.303}{t} \log \left(\frac{a}{a-x} \right) \rightarrow \textcircled{4}$$

Ex:

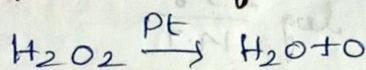
Some common reactions ^{which} follows first order kinetics ~~are~~ following:

1. decomposition of N_2O_5 in CCl_4 solution:



Nitrogen Pentoxide in CCl_4 solution decomposes to form oxygen gas decomposition

of H_2O_2 decomposition of H_2O_2 in aqueous solution:



Hydrogen peroxide in the presence of Pt as catalyst is a first order reaction

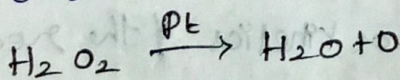
The progress of the reaction titrating equal volume of the mixture against standardised $KMnO_4$ soln at different time intervals.

Problem: 1

A solution of H_2O_2 when titrated against $KMnO_4$ soln. at different time intervals gave the following results.

t (minutes)	0	10	20
Volume $KMnO_4$ used for 10ml H_2SO_4	23.8 ml	14.7 ml	9.1 ml

Show that the decomposition of H_2O_2 is a first order reaction



Answer:

The Integrated rate equation for the first order is $k = \frac{2.303}{t} \log \left(\frac{a}{a-x} \right)$

Since the volume of KMnO_4 used in the titration is measure of conc. of H_2O_2 in solution,

Initial conc of react - $a = 23.8 \text{ ml}$

$(a-x) = 14.7 \text{ ml}$ when $t = 10 \text{ mts}$

$(a-x) = 9.1 \text{ ml}$ when $t = 20 \text{ mts}$

i) $k = \frac{2.303}{10} \log \frac{23.8}{14.7}$

$= 0.2303 (\log 23.8 - \log 14.7)$

$= 0.2303 (1.3766 - 1.1673)$

$= \underline{0.04820}$

ii) $k = \frac{2.303}{20} \log \frac{23.8}{9.1}$

$= 0.21015 (\log 23.8 - \log 9.1)$

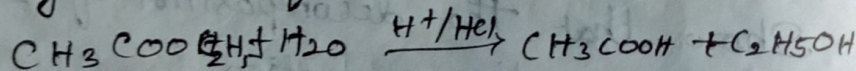
$= 0.21015 (1.3766 - 0.9595)$

$= \underline{0.0423}$

Problem 2:

Hydrolysis of an Ester:

Hydrolysis of Ethyl acetate or methyl acetate in the presence of a mineral acid as catalyst is a first order reaction.



For studying a kinetics of the reaction, a known volume of ethyl acetate is mixed with a relatively a large quantity of acid soln. at various intervals of time a known volume of the mixture is titrated against a std. alkali soln.

Hydrolysis of the Ester produces acetic acid, therefore as a reaction proceeds, the volume of alkali required for titration those on increasing

t Csec	0	4500	7140	∞
Volume of alkali used	24.36	29.32	31.72	47.15

The following about data was obtained on hydrolysis of Ethyl acetate at 20°C in 0.35N HCl established that it is a first order reaction.

Answer:

for a ~~solid~~ first order reaction

$$k = \frac{2.303}{t} \log \left(\frac{a}{a-x} \right)$$

$$a = 47.15 - 24.36 = 22.79 \text{ ml}$$

$(a-x)$ after 4500 sec

$$= 47.15 - 29.32 = 17.83 \text{ ml}$$

$(a-x)$ after 7140 sec

$$= 47.15 - 31.72 = 15.43 \text{ ml}$$

$$k = \frac{2.303}{4500} \log \frac{22.79}{17.83}$$

$$= 0.00005455$$

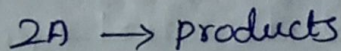
~~Since also~~

$$k = \frac{2.303}{7140} \log \frac{22.79}{15.43}$$

$$= 0.00005446$$

Since the values of t in the two experiments are fairly constant the reaction is of the first order.

✓ For a Second order reaction derivation:



$$-\frac{dx}{dt} = k(a-x)^2 \rightarrow \text{①}$$

Suppose the initial concentration a is a moles per litre.

After time t the x moles of

we know that for second order reactions, the rate of reaction is proportional to square of the conc. of the reactant.

k is the rate constant

Rearranging equ (1), we get:

$$-\frac{dx}{(a-x)^2} = k dt$$

On integration the equation two it gives,

$$-\int \frac{dx}{(a-x)^2} = k \int dt$$

$$-\int (a-x)^{-2} dx = k \int dt$$

$$-\frac{(a-x)^{-2+1}}{-2+1} = kt + I$$

$$-\frac{(a-x)^{-1}}{-1} = kt + I$$

$$+ (a-x)^{-1} = kt + I$$

$$\frac{1}{(a-x)} = kt + I \rightarrow \text{③}$$

I is the Integrated constant.

Putting $x=0$ and $t=0$,

$$I = \frac{1}{a} \rightarrow \text{④}$$

Substituting for I in eqn (3)

$$\frac{1}{a-x} = kt + \frac{1}{a}$$

$$kt = \frac{1}{(a-x)} - \frac{1}{a}$$

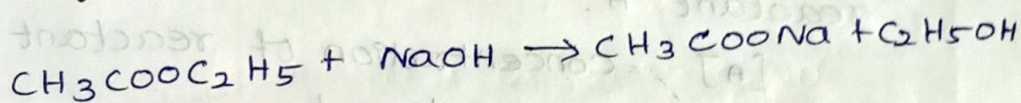
Thus,

$$k = \frac{1}{t} \left(\frac{a-a+x}{a(a-x)} \right)$$

$$k = \frac{1}{t} \left(\frac{x}{a(a-x)} \right)$$

Ex of second order reaction

1. Hydrolysis of an Ester by NaOH:



Units of zero order rate constant:

$$\text{Thus the units of } k = \frac{\text{mol}}{\text{time}} \times \frac{1}{\text{time}}$$

Time may be mole⁻¹ time⁻¹

Units of first order rate constant:

$$k = \text{time}^{-1}$$

Units of second order rate constant:

$$\frac{\text{mole}}{\text{time}} \times \frac{1}{\text{time}} \quad k = \text{mole}$$

Half life of a first order reaction:

$$t_{1/2}$$

Reaction rates can also be expressed in terms of half life

It is defined as the time required for the concentration of a reactant to decrease to half its initial value.

In other words, half life is time required of one half of the reaction to be completed. It is represented by the symbol $t_{1/2}$ (or) $t_{0.5}$

✓ Half-life of a Reaction

The Integrated first order rate eqn;

$$k = \frac{2.303}{t} \log \frac{[A]_0}{[A]}$$

where, $[A]_0$ = initial concentration of reactant A.

$[A]$ = concentration of reactant A at any time t .

Half life, $t_{1/2}$ of $[A] = \frac{1}{2} [A]_0$

Substituting values in Eqn (1)

we have

$$k = \frac{2.303}{t_{1/2}} \log \frac{[A]_0}{\frac{1}{2} [A]_0} = \frac{2.303}{t_{1/2}} \log 2$$

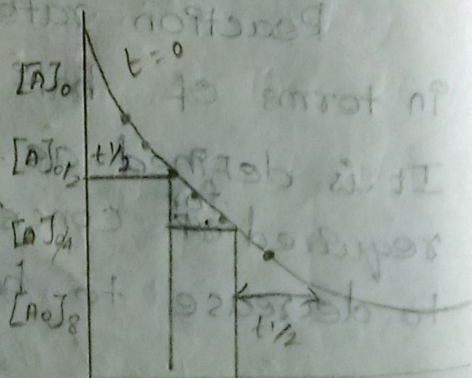
$$(or) t_{1/2} = \frac{2.303}{k} \log 2$$

$$= \frac{2.303}{k} \times 0.3010$$

$$(or) t_{1/2} = \frac{0.693}{k}$$

$t_{1/2} \Rightarrow$ Independent of Initial concn.

$$t_{1/2} \propto \frac{1}{k}$$



✓ According to this theory the chemical reaction takes place only by collision between the reacting molecules but not all collisions are effective. Only a small fraction of the collisions produce a reaction.

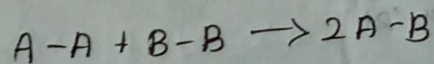
The two main conditions for a collision between the reacting molecules to be productive are;

1) The colliding molecules must possess sufficient kinetic energy to cause a reaction

2) The reacting molecules must collide with proper orientation.

3) The molecule must collide with sufficient

Let us consider a reaction



A chemical reaction occurs by breaking bonds between the atoms of the reacting molecules and forming a new bonds in the product molecules. The energy for the breaking of bonds comes from the kinetic energy (activation energy) possessed by the reacting molecules before the collision.

Fig 1 (a) (b) shows the energy of molecules A_2 and B_2 as the reaction progresses.

The fig a and b also shows the activation energy $[E_a]$ is the minimum energy

necessary to cause ^{a separation} between the colliding molecules. only the molecules collide with a kinetic energy greater than activation energy are able to get over the barrier and react. The molecules collide with kinetic energy less than $[E_a]$ E_a fail to surmount the barrier the collision between them are unproductive and the molecules simply bounce off.

collision rate $\propto [A_2][B_2]$

collision rates directly proportional to the number of molecules per litre per second.

$$CR = z [A_2] [B_2] \rightarrow \textcircled{1}$$

where z is collision proportionality factor.

② Rate directly proportional to f
where f fraction of the effective collision
with correct activation energy

$$\text{Rate} \propto f \rightarrow \textcircled{2}$$

$$f = \frac{-E_a}{RT}$$

2) The molecules must collide with proper orientation:

The reactant must collide with favorable orientation. The correct orientation, is ensure direct contact between the atom involves with breaking and forming.

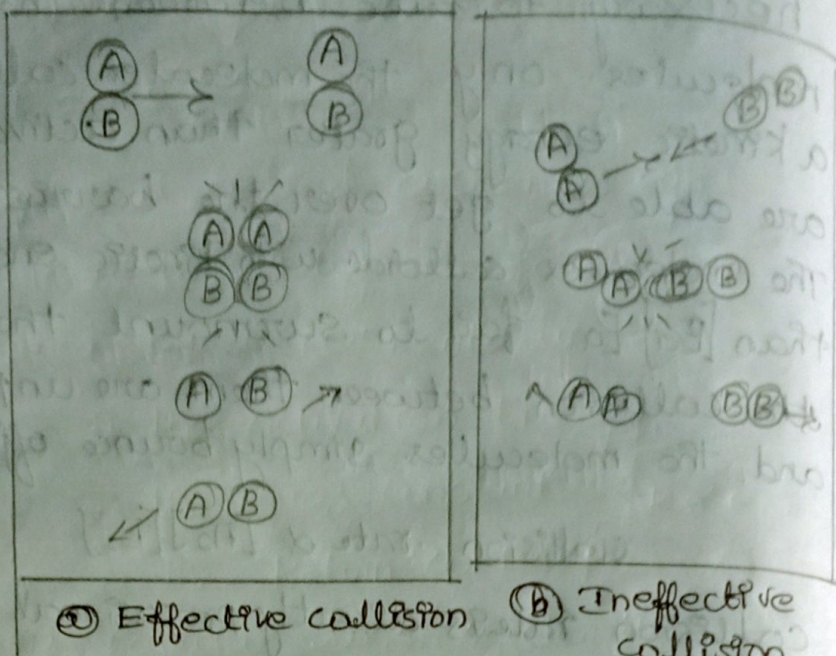


Fig: 2 orientation of reactive molecules A_2 & B_2 leads to (a) & (b)

From the above discussion of collision theory, only the molecules colliding with kinetic energy greater than E_a and with correct orientation can cause reaction.

Therefore, the rate of reaction depends on orientation of reacting molecules A_2 and B_2 with effective collision

i.e., $\boxed{\text{Rate} \propto p}$ — (1)

where p = steric factor
depends on correct orientations of A_2 & B_2

From equation (1) (2) and (3) the rate of reaction from the collision theory

$\boxed{\text{Rate} = p \times f \times CR}$ — (4)

Substituting equation (1), (2), (3) to (4)

$\boxed{\text{Rate} = p \times e^{-\frac{E_a}{RT}} \times z [A_2][B_2]}$

From rate law

$$\text{Rate} = k [A_2][B_2] \quad \text{--- (5)}$$

from eqn (4) and (5);

final form

$$k = p e^{-\frac{E_a}{RT}} z \quad \text{--- (6)}$$

Eqn (6) is the rate constant of the bimolecular reaction from the collision theory.

Effect of Increase of Temperature on Reaction Rate.

Temperature depends of reaction rate and arrhenius equation:

It is found that, the rate of reaction increases with increase of Temp. As a rule, an increase of Temp. by 10°C doubles the reaction rate, generally the increase of temp. leads to \uparrow the kinetic energy of colliding molecules.

Arrhenius Equation:

We know that the K.E of a gas is \propto to its temp. As the Temp of the system is \uparrow , more and more molecules will acquire and acquire and necessary energy greater than E_a to called ~~as~~ productive collision. This increase \leftarrow the rate of reaction.

In 1889, Arrhenius suggested simple relationship between the rate constant k for a reaction and the temp. of the system,

Arrhenius Equation :-

$$k = A e^{\frac{-E_a}{RT}} \quad \text{--- (1)}$$

The eqn (1) is called Arrhenius eqn where A is the frequency factor, are determined by experimentally.

E_a is the Activation Energy.

R is the Gas constant

T is the Kelvin temp.

$$k \propto e^{\left(\frac{-E_a}{RT}\right)}$$

$$k = A e^{\left(\frac{-E_a}{RT}\right)}$$

Eqn (1) is Arrhenius eqn

Taking natural logs each side of Arrhenius eqn (1)

$$\ln k = \ln \left[A \cdot e^{\left(\frac{-E_a}{RT}\right)} \right]$$

$$\ln k = \ln A + \ln e^{\left(\frac{-E_a}{RT}\right)}$$

$$\ln k = \ln A - \frac{E_a}{RT} \log_e e^{\left(\frac{-E_a}{RT}\right)}$$

Arrhenius Equ

$$\ln k = \ln A - \frac{E_a}{RT} (\log_e e)$$

$$\ln k = \ln A - \frac{E_a}{RT} \left(\frac{1}{T}\right) \rightarrow \text{--- (2)}$$

At two different Temperature

(i) At $T = T_1, k = k_1$

$$\ln k_1 = \ln A - \frac{E_a}{R} \left(\frac{1}{T_1}\right) \rightarrow \text{--- (3)}$$

(ii) At $T = T_2, k = k_2$

$$\ln k_2 = \ln A - \frac{E_a}{R} \left(\frac{1}{T_2}\right) \rightarrow \text{--- (4)}$$

Equ (4) - (3) :

$$\ln k_2 = \ln A - \frac{E_a}{R} \left(\frac{1}{T_2} \right)$$

$$\ln k_1 = \ln A - \frac{E_a}{R} \left(\frac{1}{T_1} \right)$$

$$\ln k_2 - \ln k_1 = -\frac{E_a}{R} \left(\frac{1}{T_2} - \frac{1}{T_1} \right)$$

$$\ln \left(\frac{k_2}{k_1} \right) = \frac{E_a}{R} \left(\frac{1}{T_1} - \frac{1}{T_2} \right)$$

$2.303 \log \left(\frac{k_2}{k_1} \right) \Rightarrow$

$$\log \left(\frac{k_2}{k_1} \right) = \frac{E_a}{2.303 R} \left[\frac{T_2 - T_1}{T_1 T_2} \right] \rightarrow (5)$$

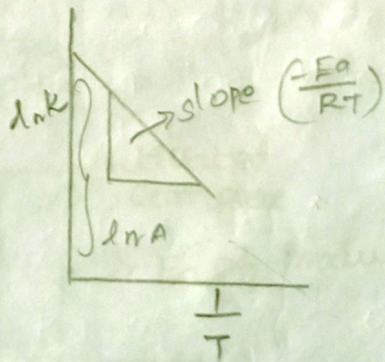
Equ (5) is Arrhenius equ for two diff Temp.

From graph: Equ (2) - slightly modified in the form of $y = mx + c$ (straight line)

$$\ln k = \ln A - \frac{E_a}{R} \left(\frac{1}{T} \right)$$

$$\ln k = \left(-\frac{E_a}{R} \right) \frac{1}{T} + \ln A$$

$$y = mx + c$$



$$\text{slope} = -\frac{E_a}{R}$$

$$\text{Intercept} = \ln A$$

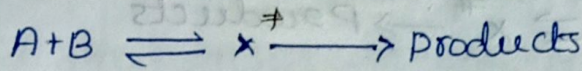
Note: $\ln = \log_e$

$$\therefore \log_e e = 1$$

$$\log = \log_{10}$$

ARRT (Absolute Reaction Rate theory)

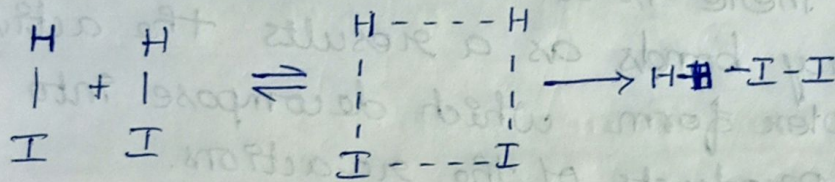
Activated complex theory (or) Transition State Theory



Reactants Activated
Complex

i.e., examples:

(Dissociation of HI & formation of products)



(Two molecules with sufficient energy come close to each other)

Redistribution of bonds and energy

Reactants

Activated Complex

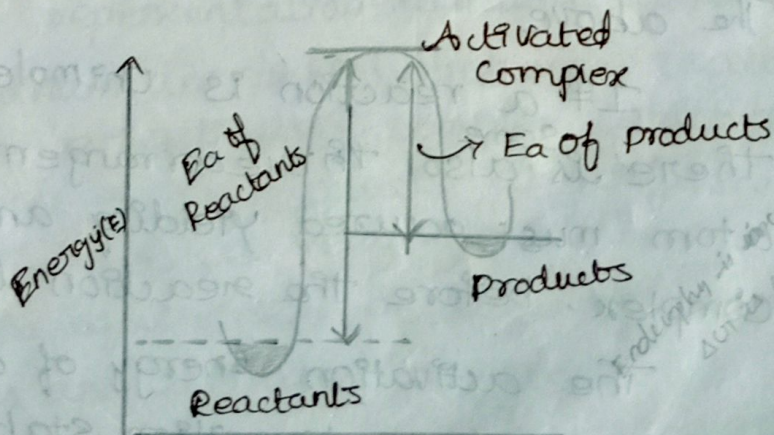


Fig: Activation energy required for the formation of activated complex.

Activation energy is calculated from the activated complex

Energy barrier

very important theory

The reactant to cross the energy barrier to form products

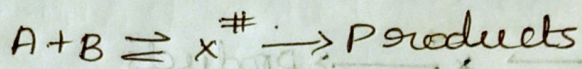
Spontaneous reaction formation of a product state that state

Endothermic reaction as energy is absorbed

Exothermic reaction as energy is released

Energy barrier is increase or decrease

By a Bimolecular reaction between a molecule a and b the steps involved are represented below. :



Reactants Activated
 complex.

The reacting molecules possessing sufficient energy approach each other and there is a redistribution of valency bonds as a result the activated complex form which decompose into the products of the reactions.

For example,

The dissociation of HI into H_2 and I_2 , the formation of the activated complex and its decomposition into products are represented by the above

If a reaction is unimolecular there is also ^{some} rearrangement of atoms must occur yielding an activated complex, before the reaction proceeds.

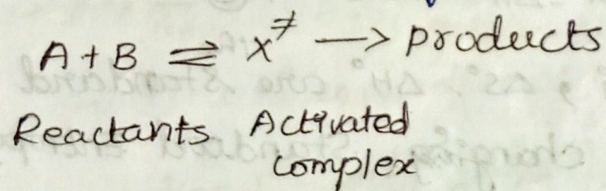
The activation energy of a reaction is important in transition state theory which is defined as the additional energy used to the reactant molecule to form intermediate activated complex for the reaction.

The small initial fall in the potential energy is due to approach of reactant molecules closed to one another, before reacting to form the activated complex similarly, the small final rises in energy of the products is due to falling apart of the products.

From the graph the energy of products higher than the reactants, the reaction is Endothermic. However, the products have less than energy than the reactant, the reaction is Exothermic.

Derivation of rate constant: (ARRT)

A bimolecular second order reaction consider to occur the following manner.



In this representation, it is assumed that an equilibrium exists between reacting molecules and activated complex which then decomposes to give products at definite rate. The rate is very slow doesn't affect the equilibrium between the reacting molecules and activated complex.

Applying Statistical Mechanics: relation bet.
Temp. & bel and
Kinetic Energy
difference.

Eyring showed;

The rate constant k of a given reaction given by

$$k = \frac{RT}{Noh} k^* \quad \text{--- (1)}$$

k^* → equilibrium constant for
 reactant convert into activated
complex.
 rate of reaction depend on the
 formation of activated complex.

Where R = gas constant

T = Absolute Temperature

N_0 = Avogadro Number

h = Plank constant

From Thermodynamics:

Standard State $\Delta G^\circ = -RT \ln k \rightarrow \textcircled{1}$
natural log

and $\Delta G^\circ = \Delta H^\circ - T\Delta S^\circ \rightarrow \textcircled{2}$

where ΔG° , ΔS° , ΔH° are ^{the} standard free energy change, standard Entropy change, standard Enthalpy change.

k = Equilibrium constant.

Eqn (2) may also written as,

$$k = e^{-\frac{\Delta G^\circ}{RT}} \rightarrow \textcircled{3}$$

Sub. ΔG° from Eqn (2) in Eqn (3):

we get Eqn (5)

$$k = e^{-\frac{\Delta H^\circ}{RT}} e^{\frac{\Delta S^\circ}{R}} \rightarrow \textcircled{4}$$

Eqn (4) written as:

$$k^* = e^{-\frac{\Delta G^\circ}{RT}} \rightarrow \textcircled{5}$$

$$k^* = e^{-\frac{\Delta H^\circ}{RT}} e^{\frac{\Delta S^\circ}{R}} \rightarrow \textcircled{6}$$

In eqn (6) and (7), ΔG^* , ΔH^* and ΔS^* are Standard energy of activation, Standard enthalpy activation and Standard Entropy of activation, respectively all are represent thermodynamic function for activated complex different from reactant at standard state of unit activity.

The value of k^* from eqn (6) in eqn (7)

we get,

$$k = \frac{RT}{N_0 h} \left[e^{-\frac{\Delta G^*}{RT}} \right] \quad \text{--- (8)}$$

disorder of the system is calculated by entropy

$$= \frac{RT}{N_0 h} \left[e^{-\frac{\Delta H^*}{RT}} e^{\frac{\Delta S^*}{R}} \right] \quad \text{--- (9)}$$

Since, $\frac{R}{N_0} = k_B$ (Boltzmann constant),

Eqn (9) written as follows,

$$k = \frac{k_B T}{h} \left[e^{-\frac{\Delta H^*}{RT}} e^{\frac{\Delta S^*}{R}} \right] \quad \text{--- (10)}$$

from eqn (9) and (10); $\frac{RT}{N_0 h}$ and $\frac{k_B T}{h}$ are constant independent of reactants and products.

if ΔH^* is close to energy of activation (E_a); eqn (10) written as follows:

$$k = \frac{k_B T}{h} \left[e^{-\frac{\Delta H^* + E_a}{RT}} e^{\frac{\Delta S^*}{R}} \right] \quad \text{--- (11)}$$

On comparing eqn (11) with Arrhenius

eqn. $k = A e^{-E_a/RT} \quad \text{--- (12)}$

The eqn ① and ② are identical if the frequency factor A put as

$$A = \frac{k_B T}{h} e^{\Delta S^\ddagger / R} \quad \text{--- ③}$$

Eqn ① compare with eqn of the collision theory.

$$k = p z e^{-E_a / RT} \quad \text{--- ④}$$

Its follows that

$$p z = \frac{k_B T}{h} e^{\Delta S^\ddagger / R} \quad \text{--- ⑤}$$

$$\text{or } p = \frac{k_B T}{z h} e^{\Delta S^\ddagger / R} \quad \text{--- ⑥}$$

In eqn ⑥ The p is probability factor introduced as a correction term in the rate constant eqn. derived from collision theory. is related to the entropy of activation, ΔS^\ddagger .

Comparison of collision theory and Transition state theory:

In collision theory equation the factor A found to be related to z , the number of collision taking place per unit volume per second. that is i.e., $A = z$.

where as in the activated complex theory, A is different meaning which is connected to entropy of activation.

However, the reaction involving simple molecules the value of A found to be same.

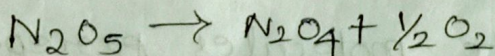
as z . Therefore the reactions involving simple molecules, the two theory^s are identical

However for the reaction involving complex molecules where the collision theory fails, the transition state theory is useable and yields satisfactory results in agreement with experiments. The transition state theory is superior to the simple collision theory. The reason is that when the reacting molecules are complex i.e. they contain large number of atoms, the formation of E_a activated complex is accompanied by a large decrease in Entropy. The quantity $e^{\Delta S^\ddagger/R}$ in eqn (10) is small in all such cases. but the $k_B T/h$ is universal constant remains same for all reactions. It follows that the frequency factor A in eqn (11) is much smaller in complex reactions. which is also less than the value of z by a factor as large as 10^6 . The probability factor P introduced derived from collision theory of reactions rate.

Lindemann's Hypothesis (or)

collision theory and Unimolecular reactions

The decomposition of Nitrogen Pentoxide;



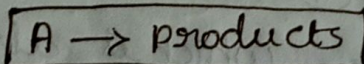
which is some difficulties in applying in collision theory to a truly unimolecular reactions.

For collision to occur at least two molecules of the same gases (or) different gases, the reaction can't be truly unimolecular. So the collision theory can't be applied to unimolecular reactions.

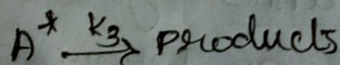
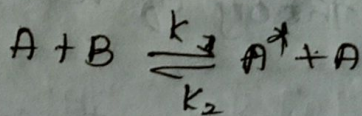
In order to explain anomaly of the unimolecular reactions

Lindemann's proposed a new hypothesis, according to which there is a time-lag between activation by collisions and subsequent reaction. During this time lag, the activated molecules are also likely to lose the excess energy and not react. However if they do not lose the excess energy and they will react.

Consider a unimolecular reaction of the type



According to Lindemann's, it will take place in the following stage:



The first stage involving collision of molecules. The formation of a few activation molecules is represented by A^* molecules.

$k_1 \rightarrow$ is the rate constant of this reaction.

Then there is some time-lag, during this interval the activated molecules may lose the excess energy and revert to the original state, k_2 is the rate constant of this reverse process as shown.

Alternatively, the activated molecules may react and decompose into the products k_3 is the rate constant of these reaction. which is follows from the above eqn.

* Rate of formation of activated molecules = $k_1[A]^2$ and

* Rate of disappearance of activated molecules = $k_2[A^*][A] + k_3[A^*]$

Here, we may apply to "steady state approximation". According to this, whenever a short lived reaction-Intermediate occurs in a system, its rate of formation can be taken as equal to its rate of disappearance. Applying this approximation

$$k_1[A]^2 = k_2[A^*][A] + k_3[A^*]$$

$$= [A^*](k_2[A] + k_3) \quad \text{--- (1)}$$

Therefore,

$$[A^*] = \frac{k_1[A]^2}{k_2[A] + k_3} \quad \text{--- (2)}$$

Since the rate of reaction is proportional to the ^{conc.} of the activated molecules, it follows that

$$r = -\frac{d[A]}{dt} = k_3[A^*]$$

Then substitute the value of A^* ^{from} in eqn (2) in eqn (3) we get, (4) eqn.

$$-\frac{d[A]}{dt} = \frac{k_1 k_3 [A]^2}{k_2 [A] + k_3} \quad \text{--- (4)}$$

Condition: 1 $k_3 \ll k_2 [A]$

When k_2 is very small in comparison to, if the conc. of A is very high

$$-\frac{d[A]}{dt} = \frac{k_1 k_3 [A]^2}{k_2 [A]} \\ = k' [A] \quad \text{--- (5)}$$

$$k' = k_1 k_3 / k_2$$

from eqn. (5) indicate reaction follows 1 order

Condition: 2

If $[A]$ is high $k_3 \gg k_2 [A]$

If k_2 is very much greater than.

Then eqn (4) converted into eqn (6)

$$-\frac{d[A]}{dt} = \frac{k_1 k_3 [A]^2}{k_3}$$

$$-\frac{d[A]}{dt} = k_1 [A]^2 \quad \text{--- (6)}$$

The reaction follows Second order from the eqn (6) if the conc. is low.

$$[A]_t = \frac{[A]_0}{1 - k_1 t [A]_0}$$