## SUDHARSAN COLLEGE OF ARTS AND SCIENCE

## Perumanadu, Pudukottai-622 104.

Model Test - II - April- 2020

## DIFFERENTIAL EQUATIONS AND LAPLACE TRANSFORMS

Class: I B.Sc (Maths)

Sub Code:16SCCMM3

Time: 3 Hours

**Marks** : 75

(10x2=20)

## Answer All questions.

- 1. Solve:  $p^2 5p + 6 = 0$ .
- 2. Solve :  $x^2 = (1 + p^2)$ .
- 3. Solve :  $(D^2 5D + 6)y = 0$ .
- 4. Find the particular integral of  $(D^2 + 5D + 6)y = e^x$
- 5. From a partial differential equation by eliminating a,b from  $z = ax + by + a^2 + b^2$ .
- 6. Solve pq = 1.
- 7. Solve:  $(D^2 + DD' 2D'^2)z = 0$ .
- 8. Solve:  $(D^2 + 3DD' + 2D'^2)z = x + y$ .
- 9. Find  $L[te^{-at}]$ .
- 10. Find  $L^{-1}\left[\frac{S^2-9}{(S^2+9)^2}\right]$ .

Part - B (5x5=25)

Answer any one choice given the each questions.

11. a) Solve 
$$:x^2p^2 + xyp - 6y^2 = 0$$

(or)

- b) Solve  $x = y + a \log p$
- 12. a) Solve :  $(D^2 4D + 3)y = \sin 3x \cos 2x$

(or)

b) Solve :
$$(D^3+8)y = x^4 + 2x + 1$$

13. a) Solve 
$$(y + z)p + (z + x)q = x + y$$
 (or)

- b) Solve  $q = xp + p^2$
- 14. a) Solve  $(D^2 DD') z = \sin x \sin 2y$

(or)

- b) Solve  $(D^2 DD' + D'^2) z = 2x + 3y$ .
- 15. a) Find  $L^{-1}\left[\frac{S+2}{(S^2+4S+5)^2}\right]$

or)

b) Find 
$$L^{-1} \left[ \frac{S^2 - S + 2}{S(S - 3)(S + 2)} \right]$$
.

Part - C (3x10=30)

Answer Any Three questions only.

- 16. Solve the equation  $\frac{d^2y}{dx^2} + y = \sec x$  Using Method of variation of parameters
- 17. Solve :  $(D^2 3D + 2)y = 540 x^3 e^{-x}$ .
- 18. Solve by Charpit's method pxy + pq + qy yz = 0.
- 19. Solve:  $(D^2 3DD' + 2D'^2)z = e^{2x-y} + e^{x+y} + \cos(x+2x)$
- 20. Solve :  $\frac{d^2y}{dt^2} + 2\frac{dy}{dt} + 5y = 4e^{-t}$  given that  $y = \frac{dy}{dt} = 0$ , when t=0