

# RELATIONAL CALCULUS

- Relational Algebra is a PROCEDURAL LANGUAGE

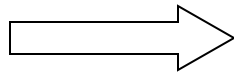
= > we must explicitly provide a sequence of operations to generate a desired output result

- Relational Calculus is a DECLARATIVE LANGUAGE

= > we specify what to retrieve, not how to retrieve it

Declarative ~ Non-Procedural

- TUPLE Relational Calculus }  
Domain Relational Calculus } Two variants of relational calculus



Both based on 1<sup>st</sup> order predicate calculus

# RELATIONAL CALCULUS

If a retrieval can be specified in the relational calculus, it can be specified in the relational algebra, and vice versa

→ expressive power of the languages is identical

A query language L is Relationally complete if L can express any query that can be expressed in the relational calculus

## OPERATIONS in Tuple Relational Calculus


$\wedge$  - AND

$\vee$  - OR

$\neg$  - NOT

$\exists x$  – there exists  $x$

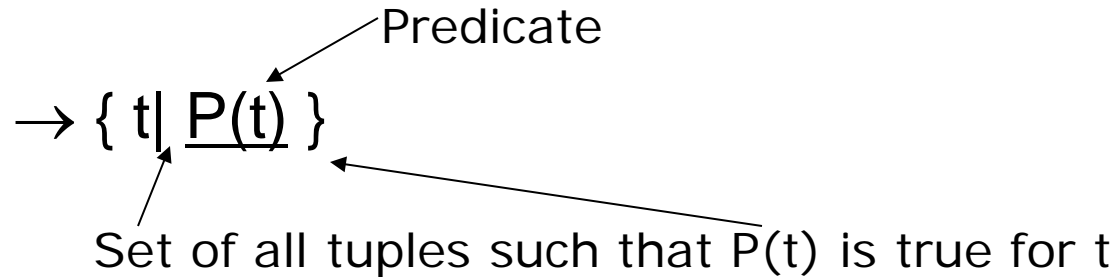
$\forall x$  – for all  $x$



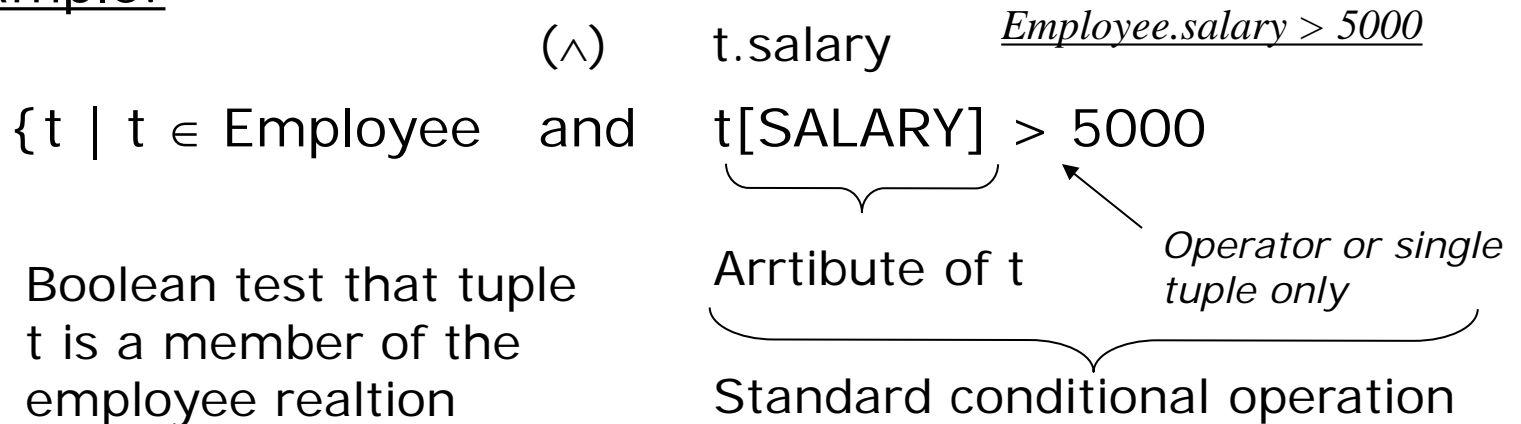
General power of  
1<sup>st</sup> order predicate  
calculus – allow  
more flexible  
expression formats

# TUPLE RELATIONAL CALCULUS

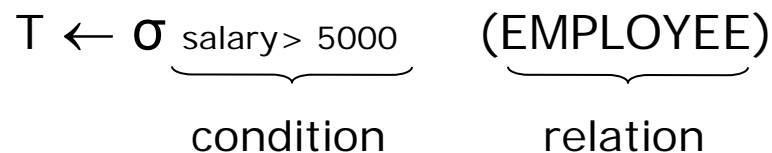
A query  
in the  
T.R.C



Example:



=> similar in function to SELECT( $\sigma$ )



# TUPLE RELATIONAL CALCULUS

## Handling Projections ( $\Pi$ )

$$\{t \mid \exists e \in \text{EMPLOYEE} (t[\text{LNAME}] = e[\text{LNAME}] \wedge e[\text{SALARY}] > 5000)$$

Projection

There exists

Select condition

(equiv to :  $\Pi_{\text{LNAME}} ( \sigma_{\text{SALARY} > 5000} (\text{EMPLOYEE}) )$ )

The new relation  $t$  is only defined for the attributes it is explicitly assigned (eg LNAME)

# JOINS IN THE TUPLE RELATIONAL CALCULUS

$$\begin{aligned}
 & \{t \mid \exists d \in \text{DEPARTMENT} \underbrace{(t[\text{DNAME}] = d[\text{DNAME}]}_{\text{projection}} \\
 & \quad \wedge \exists e \in \text{EMPLOYEE} \underbrace{(t[\text{LNAME}] = e[\text{LNAME}]}_{\text{projection}} \\
 & \quad \quad \wedge \underbrace{d[\text{MGRSSN}] = e[\text{SSN}]}_{\text{Join condition}}))\}
 \end{aligned}$$

$$\sim \Pi_{\text{DNAME, LNAME}} (\text{DEPARTMENT} \bowtie_{\text{MGRSSN=SSN}} \text{EMPLOYEE})$$


  
 Another join option

# GENERAL FORMAT OF THE TUPLE RELATIONAL CALCULUS

$\{ t \mid \exists d \in \text{DEPARTMENT} (t[\text{DNAME}] = d[\text{DNAME}]$

*Result  
relation t  
(only has  
attributes  
explicitly  
defined)*

$\wedge t[\text{DNO}] = d[\text{DNUMBER}]$

:

$\wedge d[\text{DNUMBER}] < 3$

:

$\wedge \exists e \in \text{EMPLOYEE} ( t[\text{LNAME}] = e[\text{LNAME}]$

$\wedge t[\text{FNAME}] = e[\text{FNAME}]$

$\wedge$  :

$\wedge e[\text{SEX}] = \text{M}$

$\wedge e[\text{SALARY}] < 50000$

:

$\wedge d[\text{MGRSSN}] = e[\text{SSN}] ) ) \}$

Join condition

} Project and  
rename

} Selection ( $\sigma$ ) on  
DEPARTMENT

} Project and  
rename

} Selection ( $\sigma$ )  
conditions on  
EMPLOYEE



# GENERAL FORMAT OF THE TUPLE RELATIONAL CALCULUS

{ t |  $\exists$  d  $\in$  DEPARTMENT (

$\exists$  e  $\in$  EMPLOYEE (

d[DNUMBER] < 3

$\wedge$  e[SEX] = M

$\wedge$  e[SALARY] < 50000

$\wedge$  d[MGRSSN] = e[SSN]

$\wedge$  t[DNO] = d[DNUMBER]

$\wedge$  t[DNAME] = d[DNAME]

$\wedge$  t[LNAME] = e[LNAME]

$\wedge$  t[FNAME] = e[FNAME]

)) }

} Existentialize  
Relations

} Selection ( $\sigma$ ) on  
DEPARTMENT  
And EMPLOYEE

} Join Condition(s)

} Projection

# DOMAIN RELATIONAL CALCULUS

Can represent/constraint domain/attribute values more directly

TRC:  $\{t \mid t \in \text{EMPLOYEE} \wedge t[\text{SALARY}] > 50000\}$

DRC :  $\{ \langle f, l, s \rangle \mid \langle f, l, s, b, a \rangle \in \text{EMPLOYEE} \wedge S > 50000 \}$

The "domain" values satisfying the following conditions

Attributes listed explicitly

An attribute of  $\langle \dots \rangle$

DRC :  $\{ \langle l \rangle \mid \langle f, l, s, b, a \rangle \in \text{EMPLOYEE} \wedge S > 50000 \}$

Projecting domain value for last name