

1. Let  $G$  be a group and  $a, b \in G$  then the equation  $ax=b$  and  $ya=b$  have unique solution for  $x$  and  $y$  in  $G$ .

2. Let (i)  $a^m a^n = a^{m+n}$ ,  $m, n \in \mathbb{Z}$

(ii)  $(a^m)^n = a^{mn}$ ,  $m, n \in \mathbb{Z}$

3. The union of two subgroups of Group  $G$  is a group if and only if one is contained in the other.

4. Let  $A$  &  $B$  be two subgroups of a group  $G$ . Then  $AB$  is a subgroup of  $G$  if and only if  $AB=BA$ .

5. Any subgroup of a cyclic group is cyclic.

6. Let  $G$  be a group and  $a, b \in G$  then

(i) Order of  $a =$  Order of  $a^{-1}$

(ii) Order of  $a =$  Order of  $b^{-1}ab$

(iii) Order of  $ab =$  Order of  $ba$ .

7. Let  $H$  be a subgroup of  $G$ . The number of left cosets of  $H$  is the same as the number of right cosets of  $H$ .

8. A group  $G$  has no proper subgroups if it is a cyclic group of prime order.

9. Let  $H$  and  $K$  be two subgroups of  $G$  of finite index in  $G$ . P.T  $H \cap K$  is a subgroup of finite index in  $G$ .
10. S.T If a group  $G$  has exactly one subgroup  $H$  of given order then  $H$  is a normal subgroup of  $G$ .
11. If  $G$  is a group and  $G'$  is a set of the binary operation  $\otimes$  there exist a one to one mapping  $f$  from  $G$  onto  $G'$  such that  $f(ab) = f(a) \otimes f(b) \forall a, b \in G$  then S.T  $G'$  is also a group.
12. Explain Cayley's thm
13. Explain Fermat's thm
14. S.T  $|H|$  divides  $|G|$
15. Let  $G$  be a group. Then the order of  $a$  is same as the order of cyclic group generated by  $a$ .
16. Let  $G$  be a group and  $H$  be a subgroup of  $G$ , then
- (i)  $a \in H \Rightarrow aH = H$
  - (ii)  $aH = bH \Rightarrow a^{-1}b \in H$
  - (iii)  $a \in bH \Rightarrow a^{-1} \in Hb^{-1}$
  - (iv)  $a \in bH \Rightarrow aH = bH$
17. Let  $H$  &  $K$  be two subgroups of  $G$  of finite index in  $G$ . P.T  $H \cap K$  is a subgroup of finite index in  $G$ .

18. Let  $N$  be a subgroup of  $G$ . Then the

following are equivalent

(i).  $N$  is a normal subgroup of  $G$ .

(ii).  $aNa^{-1} = N \quad \forall a \in G$

(iii).  $aNa^{-1} \subseteq N \quad \forall a \in G$

(iv).  $aNa^{-1} \cap N \neq \emptyset \quad \forall n \in N \text{ \& } a \in G$ .

19. Let  $N$  be a normal subgroup of  $G$  then

$G/N$  is a group under the operation

defined by  $Na \cdot Nb = N(ab)$

20. Isomorphism is an equivalence relation

among groups.