

Operation Research:-

II-BBA

16CCBB8

Section -A

1. Define "Operation Research:-

Operation Research is a Scientific Method of providing executive departments with a quantitative basis for decisions regarding the operations under their control.

- Morse and Kimball.

2. What is Graphical Method:-

Graphical Method It is essential involves indicating the constraints on the Graph and determining the feasible region.

3. Transportation problem:-

The Transportation problem is one of the subclass of LPP's. Here quantities of a single homogeneous commodity that are initially stored at various origins to different destinations in such a way that the transportation cost is minimum.

4. Define "feasible solution:-

Any set of non-negative allocations $(x_{ij} \geq 0)$ which satisfies the row and column sum is called a feasible solution.

5. Mean by Assignment problem:-

* Suppose there are n jobs to be performed and n persons are available in doing in this job.

* assume that each person can do each job at a time through with vary degrees of efficiency

* The problem is find to an assignment, the total cost of performing all the job is minimum.

6. What is linear programming:-

It is the analysis of problem in which a linear function of a number of variables is to be optimized when the variables are subject to a number of restraints in the form of inequalities.

7. phases of Operation Research:-

* Judgement phase

* Research phase

* action phase

8. What is Decision Making:-

Decision literally means choosing from available alternatives the essential characteristics all decision are.

1. Driigger
2. Alternative at the disposal
3. Influencing factors.

9. What is Models of function:-

The model can be three categories.

(i) Descriptive Model

(ii) predictive Model

(iii) Normative or Optimization model.

10. Limitation of Operation Research:-

(i) Models are the only idealized representations of reality and cannot be regarded as absolute in any case

(ii) the validity of the Model of a particular situation of can be a only by conducting experiments.

11 Define "Inventory Control"

The American Institute of Certified Public Account (AICPA) defines "Inventory" in the sense of tangible goods which are held for sale, in process of production and available for ready consumption.

12. Meaning of Inventory Control:

It may mean stock of finished goods only. In a manufacturing concern, it may include raw materials, work in process and stores, etc. to understand the exact

Meaning of the Work inventory

13. Meaning of Replacement:

The study of Replacement is concerned with situations that arise when some items such as Machines, Men, electric-light bulbs, etc... need replacement due to their deteriorating efficiency, failure or break down.

14

Define LPP

LPP involving two decision variable can be solved Graphical the optimum solution to LPP can be evaluating the value of the Objective function.

15 What is Raw material:-

It include direct Material used in a manufacture of a product. a prepare of holding raw material is to ensure production in a event of delivery.

16 Meaning of Cost of Inventory:-

In determining and Optional inventory policy, the most often is the cost function.

(i) purchase cost

(ii) Ordering cost / set-up cost

(iii) Carrying cost

(iv) Stock out cost.

17. Probabilistic Model:-

We consider the situations where demand is not known exactly but the prob. probabilistic distribution of demand is some known.

1) Single period probabilistic Model

2) Multiperiod probabilistic Model.

18. What is Scrap Material:-

It represents the waste material produced in the process of production. Scrap is sold to secondary market so as to get some value out of it.

19. Reasons for Carrying Inventory

* Transaction Motive

* Precautionary Motive

* Speculative Motive.

20. Basic EOQ Model:-

EOQ = Economic Order Quantity

In this model, the demand is assumed to be fixed and completely pre-determined that is static demand. EOQ is an important factor controlling inventory.

Section B

5 Mark

1. Phase of Operation Research:-

The procedure to be followed in the study of operation research generally involved the following phases

- (i) formulation the problem
- (ii) Constructing a mathematical Model
- (iii) deriving the solution from the Model
- (iv) testing the Model and its Solution
(updating the Model)
- (v) Controlling the Solution
- (vi) implementation.

2. A Company Manufactures two products, A and B these products are processed in the same machine. It takes 10 minutes to process one unit of products A and 2 minutes for each unit of product B and the machine operates for a maximum of 35 hours in a week product A requires 1 kg and B requires 0.5 kg of raw material per unit, the supply of which is 600 kg per week. Market constraint on product B is known to be minimum of 800 units every week product A costs ₹ 5 per unit and is sold at ₹ 10 product B costs ₹ 6 per unit and can be sold in the market at a unit price of ₹ 8 Determine the number of units of A and B per week to maximize the profits.

Solution:-

A & B

A required 10 minutes

B required 2 minutes

maximum 35 hours

raw material:-

A required 1 kg

B required 0.5 kg

Decision variable : A & B consists of x_1, x_2

Objective Variable

Cost price A 5, Sold = 10

A price = $10 - 5 = 5x_1$

B price = $8 - 6 = 2x_2$

max $z = 5x_1 + 2x_2$

Constraints = There are two constraints
product A, product B.

Product $10x_1 + 2x_2 \leq 2100$ | 35 hours
35 x 60 = 2100

Raw material

$1x_1 + 0.5x_2 \leq 600$

$x_2 \geq 800$

Subject to:

max $z = 5x_1 + 2x_2$

$10x_1 + 2x_2 \leq 2100$

$1x_1 + 0.5x_2 \leq 600$

3. Scope of Operation Research:-

There is a great scope for economist, administrated and technician working as a team to solve the problem or deficiency by using Operation Research approach.

(i) agriculture

(ii) finance

(iii) Industry

(iv) Marketing

(v) Personal Management

(vi) production Management

(vii) Research and development

(viii) military operation.

A. Solve the LPP by Graphical Method.

$$\text{Minimize } Z = 20x_1 + 10x_2$$

Subject to

$$x_1 + 2x_2 \leq 40$$

$$3x_1 + x_2 \geq 30$$

$$4x_1 + 3x_2 \geq 60$$

$$x_1, x_2 \geq 0$$

$$(i) \quad x_1 + 2x_2 \leq 40$$

$$x_1 = 0$$

$$x_1 + 2x_2 = 40$$

$$0 + 2x_2 = 40$$

$$x_2 = \frac{40}{2} = 20$$

$$x_2 = 20$$

point (0, 20)

$$(ii) \quad x_2 = 0$$

$$x_1 + 2x_2 = 40$$

$$x_1 + 0 = 40$$

$$x_1 = \frac{40}{1} = 40$$

$$x_1 = 40$$

point (40, 0)

$$(iii) \quad 3x_1 + x_2 \geq 30$$

$$x_1 = 0$$

$$3x_1 + x_2 = 30$$

$$0 + x_2 = 30$$

$$x_2 = \frac{30}{1} = 30$$

point (0, 30)

$$x_2 = 30$$

$$x_2 = 0$$

$$3x_1 + x_2 = 30$$

$$3x_1 + 0 = 30$$

$$x_1 = \frac{30}{3} = 10$$

point (10, 0)

$$x_1 = 10$$

$$(ii) 4x_1 + 3x_2 = 60$$

$$x_1 = 0$$

$$4x_1 + 3x_2 = 60$$

$$0 + 3x_2 = 60$$

$$x_2 = \frac{60}{3} = 20$$

$$x_2 = 20$$

point (0, 20)

$$x_2 = 0$$

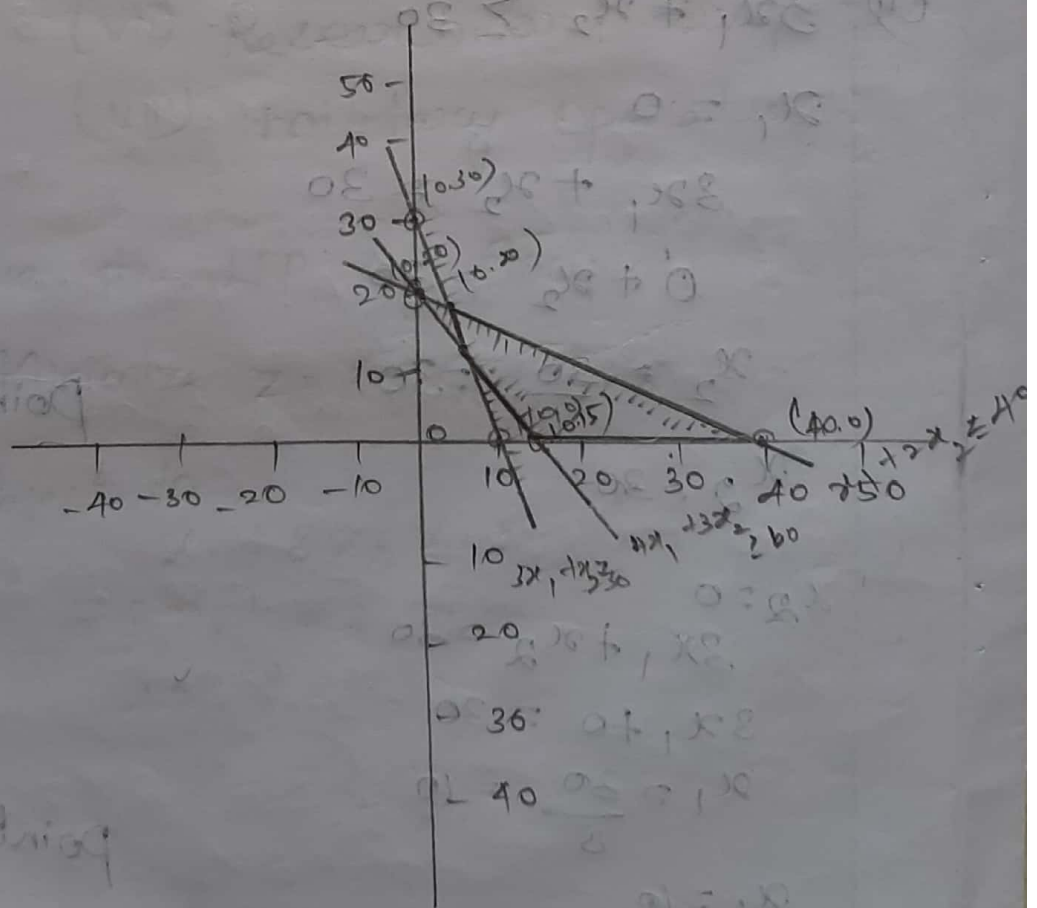
$$4x_1 + 3x_2 = 60$$

$$4x_1 + 0 = 60$$

$$x_1 = \frac{60}{4} = 15$$

$$x_1 = 15$$

point (15, 0)



$$x_1 + 2x_2 = 40 ; 3x_1 + x_2 = 30$$

$$A = (15, 0)$$

$$B = (40, 0) \quad x_1 + 2x_2 = 40 \rightarrow \textcircled{1} \times 3$$

$$C = ? \quad 3x_1 + x_2 = 30 \rightarrow \textcircled{2}$$

$$D = ?$$

$$3x_1 + 6x_2 = 120$$

$$3x_1 + x_2 = 30$$

$$\hline 5x_2 = 90$$

$$x_2 = 18$$

$$x_2 = \frac{90}{5} = 18 \quad x_2 = 18$$

$x_2 = 18 \Rightarrow$ substitute to $\textcircled{1}$

$$x_1 + 2x_2 = 40$$

$$x_1 + (2 \times 18) = 40$$

$$x_1 + 36 = 40$$

$$x_1 = 40 - 36$$

$$\boxed{x_1 = 4}$$

$$4x_1 + 3x_2 = 60 ; 3x_1 + x_2 = 30$$

$$4x_1 + 3x_2 = 60 \rightarrow \textcircled{1}$$

$$3x_1 + x_2 = 30 \rightarrow \textcircled{2} \times 3$$

$$9x_1 + 3x_2 = 90$$

$$4x_1 + 3x_2 = 60$$

$$\hline 5x_1 = 30$$

$$x_1 = \frac{30}{5} = 6$$

$$x_1 = 6$$

$$3x_1 + x_2 = 30$$

$$(3 \times 6) + x_2 = 30$$

$$18 + x_2 = 30$$

$$x_2 = 30 - 18$$

$$x_2 = 12$$

point (6, 12)

$$\text{min } z = 20x_1 + 10x_2$$

points value

$$A (15, 0) \rightarrow 300$$

$$B (40, 0) \rightarrow 800$$

$$C (4, 18) \rightarrow 200$$

$$D (6, 12) \rightarrow 240$$

$$(i) 20x_1 + 10x_2 = z$$

$$(20 \times 15) + (10 \times 0) = z$$

$$300 + 0 = 300$$

$$(ii) 20x_1 + 10x_2 = z$$

$$(20 \times 40) + (10 \times 0) = z$$

$$800 + 0 = 800$$

$$(iii) 20x_1 + 10x_2 = z$$

$$(20 \times 4) + (10 \times 18) = z$$

$$80 + 180 = 260$$

$$(iv) 20x_1 + 10x_2 = z$$

$$(20 \times 6) + (10 \times 12) = z$$

$$120 + 120 = 240$$

5. Difference between transportation problem and Assignment problem.

transportation problem	Assignment problem
<p>1. Number of sources and destinations need not to be equal the cost is not necessary for a square matrix.</p>	<p>assignment problem is done on a one-to-one basis the number sources and destination are equal, the cost matrix must be square matrix.</p>
<p>2. The problem is unbalanced if the total supply and total demand are not equal</p>	<p>The problem is unbalanced if the cost matrix is not a square matrix.</p>
<p>3. The capacity and the requirement value is equal to a_i and b_j, for the source of j^{th} destination $i = 1, 2, \dots, m$ $j = 1, 2, \dots, n$</p>	<p>The capacity and the requirement value is exactly one, that is for each source of each destination.</p>

x_{ij} , the quantity to be transported from i th origin to the j th destination can take any possible positive value.

x_{ij} the i th is to be assigned to the j th here and can take either the value one and 0 or 0

b. Explain the North West Corner Rule.

	A	B	C	supply
O1	5	6	7	9
O2	7	8	6	10
O3	2	4	3	6
Demand	5	9	11	25

	A	B	C	
O1	5	4	7	9
O2	7	5	6	10
O3	2	4	3	6
	5	9	11	25

$x_{11} = 5$

$x_{12} = 4$

$x_{22} = 5$

$x_{23} = 5$

$x_{33} = 6$

Total Cost $(5 \times 5) + (4 \times 6) + (5 \times 8) + (5 \times 6) + (3 \times 6)$

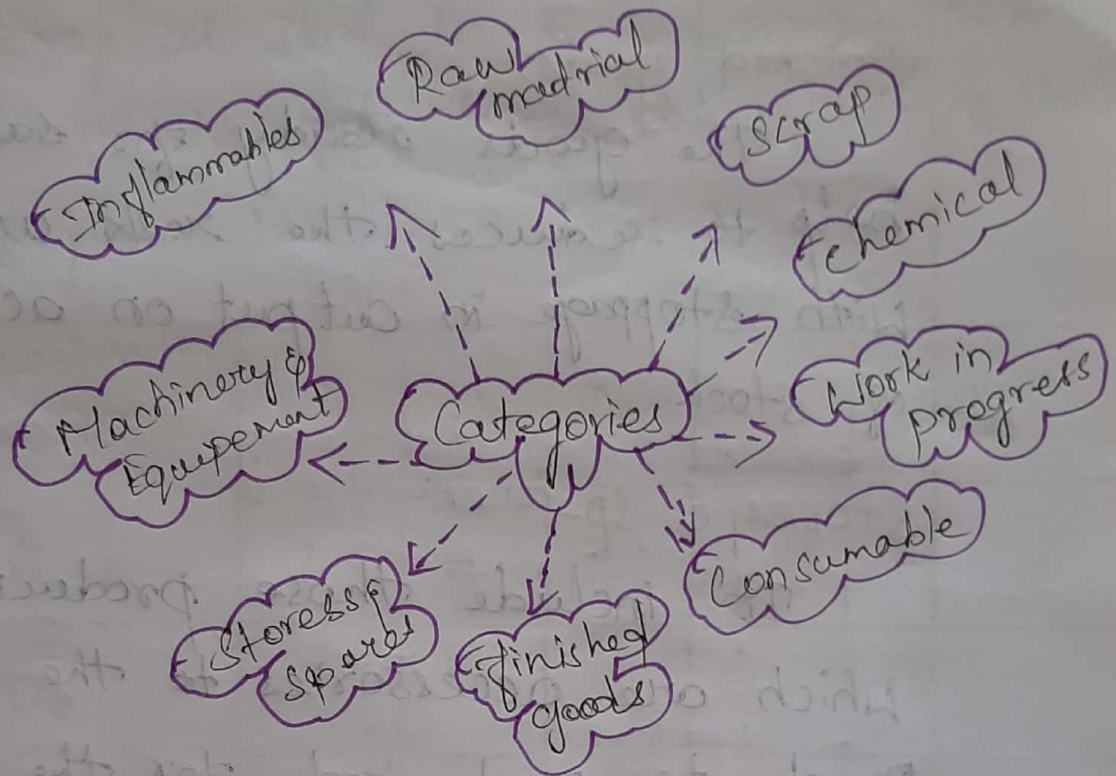
$\Rightarrow 25 + 24 + 40 + 30 + 18$

$\Rightarrow 49 + 70 + 18$

$\Rightarrow 119 + 18$

$\Rightarrow \sqrt{137}$

7 Categories of Inventory



Raw Material:-

It include direct Material used in a manufacture of a product a propose of holding raw material is to ensure production in a event of delivery

Work in progress:-

It include finished goods and Material help between manufacturing stage. It also can be raw material which are used in production process.

Consumable:-

The product are consumed buy recurrently. It is items which get used up.

finished goods:-

The goods ready for sale. It help to reduces the risk associated with stoppage in output on account of stock.

Stores & spares:-

It include those products which are accessories to the main products, produced for the purpose of sale.

Machinery & Equipment:-

All the Machinery, power and hand driven Equipment such as Electric Motors, types Writers, plate machines and other machines in used in production in other department.

Chemical:-

The should be stored preserved and issued very careful security since there use good event life to ask.

Scrap Material:-

It represents the waste material produced in the process of production. Scrap is sold to secondary market so as to get some value out of it.

8 Explain the least cost method.

Destination Origin	D ₁	D ₂	D ₃	D ₄	Supply
O ₁	6	4	1	5	14
O ₂	8	9	2	7	16
O ₃	4	3	6	2	5
dd	6	10	15	4	35

$$a_{ij} = 35 = b_{ij}$$

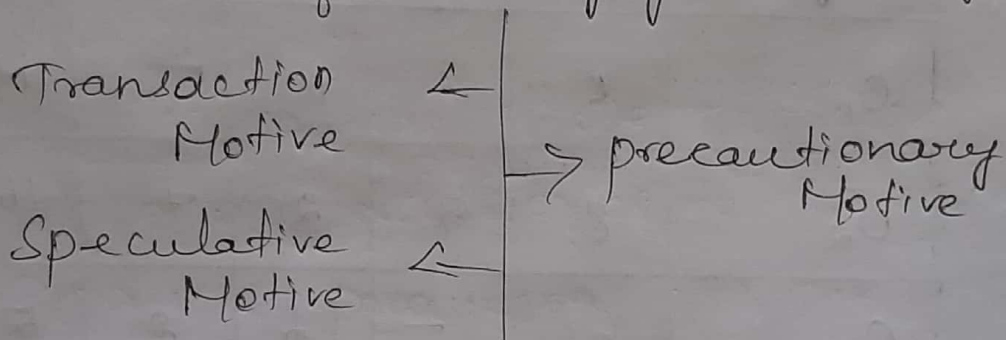
	D ₁	D ₂	D ₃	D ₄	
O ₁	6	4	14	5	14 0
O ₂	6	9	2	7	16 18 9
O ₃	4	3	6	2	5 1
	6	10	15	4	
	0		1		

$x_{13} = 14$
 $x_{21} = 6$
 $x_{22} = 9$
 $x_{23} = 1$
 $x_{32} = 1$
 $x_{34} = 2$

$$\begin{aligned}
 \text{Total Cost} &= (14 \times 1) + (6 \times 8) + (9 \times 9) + \\
 &\quad (1 \times 2) + (1 \times 3) + (4 \times 2) \\
 &= 14 + 48 + 81 + 2 + 3 + 8 \\
 &= 62 + 83 + 11 \\
 &= 145 + 11
 \end{aligned}$$

$$\text{least Cost} = 156/11$$

9 Reasons for carrying Inventory



Transaction Motive

Every firm has to maintain some level of inventory to meet the day to day requirements of sales, production process, customer demand, etc. This motive makes the firm to keep the inventory of finished goods as well as raw materials.

2) Precautionary Motive:-

Firm should keep some inventory for unforeseen circumstances. Also, if the fresh supply of raw material may not reach the factory due to strike by the transporters or due to natural calamities in a particular area.

3) Speculative Motive:-

The firm may be tempted to keep some inventory in order to capitalize an opportunity to make profit. e.g. sufficient level of inventory may help the firm to earn extra profit in case of expected shortage in the market.

10. Explain the Vogel's Approximation Method:-

to/from	w_1	w_2	w_3	w_4	Supply
F_1	6	4	1	5	14
F_2	8	9	2	7	16
F_3	4	3	6	2	5
d ₁	6	10	15	4	

	I	II	III	IV	V
11	4	3	3	3	1
10	4	5	1	1	1
8	9	2	7	1	1
4	3	6	2	1	1

4×6 10×4 1×8 15×9 1×4

I 2 1 1 3

II 2 1 - 3

III 2 1 - -

IV 2 1 - -

V 2 - - -

$$\begin{aligned}
 &= (4 \times 6) + (10 \times 4) + (1 \times 8) + (15 \times 9) + (1 \times 4) \\
 &\quad + (1 \times 2) \\
 &= 24 + 40 + 8 + 30 + 4 + 2
 \end{aligned}$$

total cost = $\boxed{114}$

11) Replacement policy for Equipement

That Deteriorates Gradually:

When Operational efficiency of an item deteriorates with time (gradual failure), it is economical to replace the same with a new one.

Besides there could be a number of alternative choices and one may like to compare available alternative on the basis of the running costs. Coverage maintenance and Operating Costs involved

12. Calculate EOQ:

Annual Demand = ₹ 20,000

Ordering Cost = ₹ 150 per unit

Inventory carrying Cost = 24%

$$Q^* = \sqrt{\frac{2AD}{H}} = \sqrt{\frac{2 \times 20,000 \times 150}{0.24}} = 5000$$

$$= \sqrt{\frac{2 \times 20,000 \times 150}{0.24}}$$

$$= \sqrt{\frac{40,000 \times 150}{0.24}}$$

$$= \sqrt{\frac{6,000,000}{0.24}} = \sqrt{25,000,000}$$

$$= ₹ 5000/-$$

Total cost

$$\int 2 \cdot ADh$$

$$= \int 2 \times 150 \times 20,000 \times 0.04$$

$$= \int 1,440,000$$

$$= 1200 \text{ l.}$$

13. Characteristics of Operation Research:-

- * System Orientation
- * use of inter disciplinary of terms
- * application of Scientific Method
- * uncovering new problems &
- * Quantitative solution.
- * human factors.

14. Models by the Extent of Generality

This model is divided to two

Categories.

(i) Specific

(ii) General.

Specific:-

It represent a system at some specific time. It is known as Specific Model.

General:-

Simulation and heuristic model fall under the categories of general model.

15 A firm is using a machine whose purchase price 13000 installation cost 3600 and the machine has scrap value 1600 the maintenance cost in various years

Year	1	2	3	4	5	6	7	8	9
Cost	850	1150	1000	1500	2100	2900	4000	4800	6000

The firm wants to determine after how many years should the machine replaced on economic consideration assuming the machine replacement

Ans:-

Cost of Machine = 13,000

(A) Installation = 3,600

Cost of M = $\frac{16,600}{}$

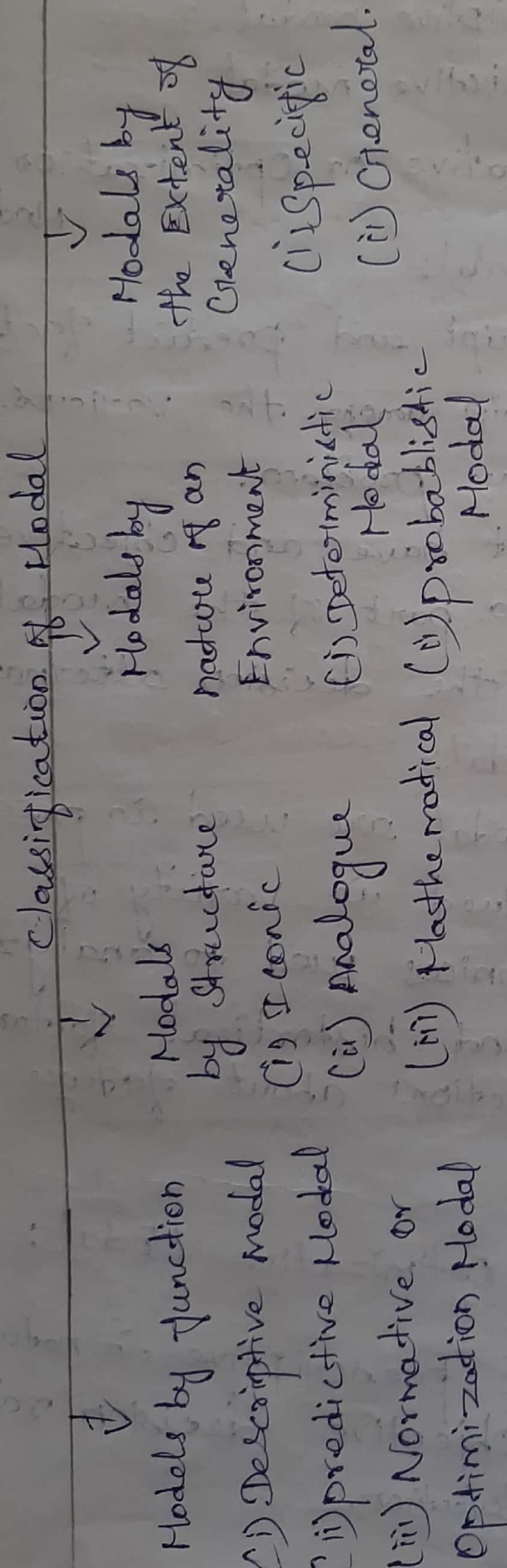
Scrap value = 1,600 (G)

1 year	2 Maintenance cost	3 Cummul	4 C-S	5 = 3+A	6 = $\frac{5}{n}$
1	250	250	15000	15250	15250
2	750	1000	15000	16000	8000
3	1000	2000	15000	17000	5666.6
4	1500	3500	15000	18500	4,625
5	2100	5600	15000	20600	4120
6	2900	8500	15000	23500	3916.6
7	4000	12500	15000	27500	3928.5
8	4800	17300	15000	32300	4037.5
9	6000	23300	15000	38300	4255.5

Solution:-

It may be minimum total average cost 3916 during 6th year therefore the Machine should be replace after every 6th years, otherwise the average cost per year would state increasing.

1. Classification of Modal:-



Models by function:-

The model can be three categories

- (i) Descriptive model
- (ii) predictive model
- (iii) Normative or Optimization Model

Descriptive Model:-

They describe and predict facts and relationship among the various activities of the problem.

They don't have an objective function as a part of the model to evaluate the decision alternatives.

Predictive model:-

These models are used in predictive analysis involved in variety of statistical techniques used to analyze the current and historical factors to make predictions about future events.

Normative (or) Optimization Model:-

They are prescriptive in nature and develop objective decision rules for optimum selection.

Models by structure:-

This Model is divided to three types.

(i) Iconic

(ii) Analogue

(iii) Mathematical.

Iconic Model:-

These are the pictorial representation of real system and have the appearance of the real thing

ex:- City map, blue print of house etc...

Analogue Model:-

They are more abstract than the iconic model as there is no similarity between these model and real life items

Mathematical Model:-

They are the most abstract in nature and employ a set of mathematical symbols to represent the components of the real system.

Models by Nature of an Environment

This model divided to two categories

(i) Deterministic Model

(ii) Probabilistic Model.

Deterministic Model

In this model all parameters and financial relationship are assumed to be known with certain decision to be made.

Probabilistic Model:-

These model have at least one parameter or decision variable as a random variable

Models by the Extent of Generality

This model is divided to two

Categories

(i) Specific

(ii) General

Specific

It represent a system at some specific time. It is known as specific model.

General:-

Simulation and heuristic model fall under the categories of General model.

Q. A Manufacture produce two type of model m_1 & m_2 . each model of the type m_1 require 4 hours of grinding and 2 hours of polishing. each model of the type m_2 require 2 hours of grinding and 5 hours of polishing

The manufacture has 2 grinders & 3 polisher each grinder work 40 hours in a week and each polisher work for 60 hours a week

profit on m_1 model is 3 Rs and m_2 model 4 Rs

two types of model make the maximum profit in a week.

Solution:-

M_1 & M_2 .

M_1 required 4 hours - grinding
 2 hours - polishing

M_1 required 2 hours - Grinding
5 hours - polishing

Grinder = 2

polisher = 3

↓ (2x40)

↓ (3x60)

40 hours

60 hours

profit $M_1 = 3₹$ $M_2 = 4₹$

Decision variables = M_1, M_2 consist for x_1, x_2

Objective Variable Max $z = 3x_1 + 4x_2$

Constraints: There are two constraints

(i) Grinder (ii) polisher

(i) first consist for Grinder (40x2)

$$4x_1 + 2x_2 \leq 80$$

(ii) second consist for polisher (60x3)

$$2x_1 + 5x_2 \leq 160$$

Solution :-

$$\max z = 3x_1 + 4x_2$$

subject to:

$$4x_1 + 2x_2 \leq 80$$

$$2x_1 + 5x_2 \leq 160$$

$$x_1, x_2 \geq 0$$

Q) Explain the transportation problem of initial stage:-

Transportation problem:-

The transportation problem is one of the subclass of LPP's. Here quantities of a single homogeneous commodity that are initially stored at various origins to different destinations in such a way that the transportation cost is minimum.

(i) feasible solutions

(ii) Basic feasible solution

(iii) Non-degenerate Basic feasible solution.

(iv) Degenerate basic feasible solution.

(i) feasible solution:-

Any set of non-negative allocations ($x_{ij} \geq 0$) which satisfies the row and column sum is called a feasible solution.

2. Basic feasible solution:-

A feasible solution is called a basic feasible solution, if the number of non-negative allocation is equal to $(m+n-1)$ where m is the number of rows and n the number of columns in a transportation table

3. Non degenerate Basic feasible solution

Any feasible solution to a transportation problem containing m origin and n destinations is said to be non-degenerate if it contains $m+n-1$ occupied cells and each allocation is an independent position.

4. degenerate basic feasible solution:-

If a basic feasible solution contains less than $m+n-1$, non negative allocation it is set to be degenerate.

Optimal Solution:-

Optimal solution is a feasible solution, which minimizes the total cost

The solution of a transportation problem can be obtained in two

(i) initial stage

(ii) Optimum solution.

(i) initial stage

* north, west corner Rule (NWCR)

* least cost Method (or) Matrix minimum Method

* Vogel's Approximation Method (VAM)

$$A) \max Z = 3x_1 + 4x_2$$

Subject to

$$5x_1 + 4x_2 \leq 200$$

$$3x_1 + 5x_2 \leq 150$$

$$5x_1 + 4x_2 \geq 100$$

$$8x_1 + 4x_2 \geq 80$$

$$x_1, x_2 \geq 0$$

$$(i) 5x_1 + 4x_2 = 200$$

$$x_1 = 0$$

$$0 + 4x_2 = 200$$

$$x_2 = \frac{200}{4}$$

$$x_2 = 50$$

$$\boxed{0, 50}$$

$$x_2 = 0$$

$$5x_1 + 0 = 200$$

$$x_1 = \frac{200}{5}$$

$$x_1 = 40$$

$$\boxed{40, 0}$$

$$(ii) 3x_1 + 5x_2 = 150$$

$$x_1 = 0$$

$$0 + 5x_2 = 150$$

$$x_2 = \frac{150}{5}$$

$$x_2 = 30$$

$$\boxed{0, 30}$$

$$x_2 = 0$$

$$3x_1 + 0 = 150$$

$$x_1 = \frac{150}{3}$$

$$x_1 = 50$$

$$\boxed{50, 0}$$

$$(iii) 5x_1 + 4x_2 = 100$$

$$x_1 = 0$$

$$0 + 4x_2 = 100$$

$$x_2 = \frac{100}{4}$$

$$x_2 = 25$$

$$\boxed{0, 25}$$

$$x_2 = 0$$

$$5x_1 + 0 = 100$$

$$x_1 = \frac{100}{5}$$

$$x_1 = 20$$

$$\boxed{20, 0}$$

$$(iv) \quad 8x_1 + 4x_2 = 80$$

$$x_1 = 0$$

$$0 + 4x_2 = 80$$

$$x_2 = \frac{80}{4} = 20$$

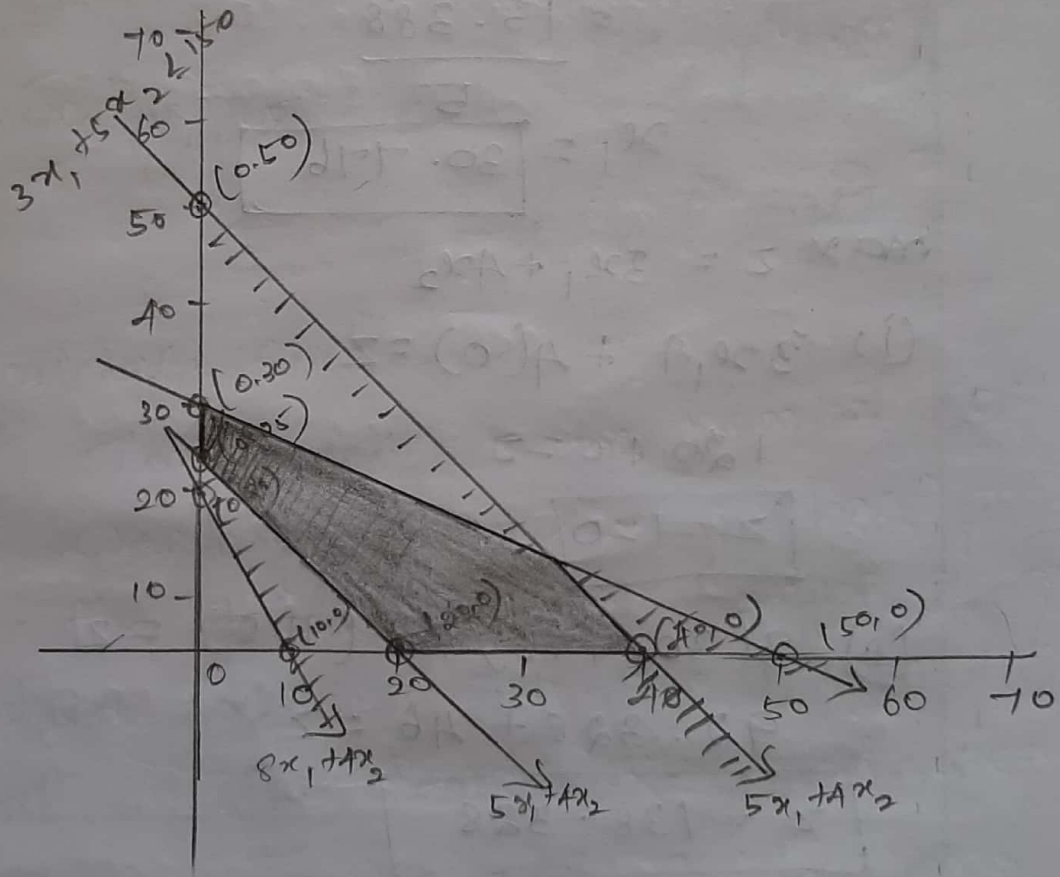
$$\boxed{0, 20}$$

$$x_2 = 0$$

$$8x_1 + 0 = 80$$

$$x_1 = \frac{80}{8} = 10$$

$$\boxed{10, 0}$$



$$5x_1 + 4x_2 = 200 \quad \text{--- (1) } \times 3$$

$$3x_1 + 5x_2 = 150 \quad \text{--- (2) } \times 5$$

$$15x_1 + 12x_2 = 600$$

$$15x_1 + 25x_2 = 750$$

$$\hline 13x_2 = 150$$

$$x_2 = \frac{150}{13} \cdot 11.53$$

$$x_2 = 11.53$$

$$5x_1 + 4x_2 = 200$$

$$5x_1 + (4 \times 11.53) = 200$$

$$5x_1 + 46.12 = 200$$

$$5x_1 = 200 - 46.12$$

$$5x_1 = 153.88$$

$$= \frac{153.88}{5}$$

$$x_1 = \frac{30.776}{5}$$

$$\text{max } z = 3x_1 + 4x_2$$

$$(i) 3x_1 + 4(0) = z$$

$$120 + 0 = z$$

$$z = 120$$

$$(ii) 3(30.776) + 4(11.5) = z$$

$$92.328 + 46 = z$$

$$z = 138.328$$

$$(iii) 3(0) + 4(30) = z$$

$$0 + 120 = z$$

$$z = 120$$

$$(iv) 3(0) + 4(25) = z$$

$$0 + 100 = z$$

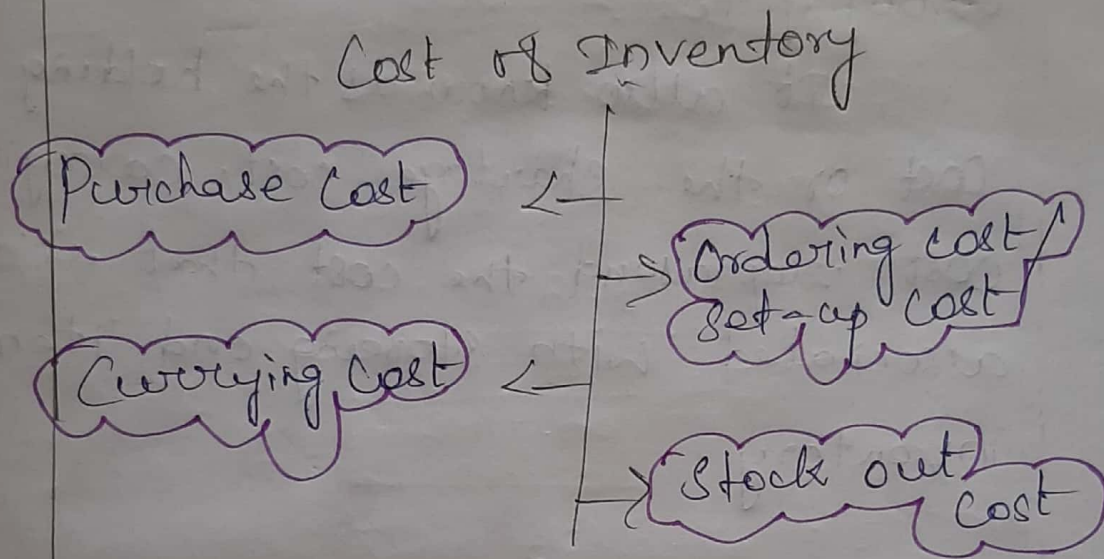
$$z = 100$$

Point are (30.776, 11.5)

$$\text{mix} = 138.328$$

5 What are inventory cost
Cost and term associated with Inventory

In determining and optimal
inventory policy, the most often is
the cost function.



purchase cost:-

This refers to the nominal cost
of inventory. It is the purchase price
for the items that are bought from
outside sources, and the production
cost. If the items are produced
within the organization. This may
be constant per unit, or, it may vary
as the quantity purchased
increase or decrease

Ordering cost / setup cost :-

It is incurred when the inventory is re-ordered. It includes cost associated with the processing and transportation, inspection and quality etc...

Carrying cost :-

It is also known as the holding cost or the shortage cost, carrying cost represents the cost that is associated with storing an item in inventory.

Stock out cost :-

Stock out cost is the cost associated with not serving the customer. Stock out is an important shortage if the shortage is internal.

b) Explain the NWCR, least cost method, and VAM method.

6	8	7	1	18
9	6	13	12	25
17	8	5	4	30
30	10	15	18	73

NWCR

<u>18</u>				18
6	8	7	1	
<u>12</u>	<u>10</u>	<u>3</u>		25 13
9	6	13	12	
17	8	<u>12</u>	<u>18</u>	30 18
30	10	15	18	
12		12		

$$x_{11} = 18$$

$$x_{21} = 12$$

$$x_{22} = 10$$

$$x_{23} = 3$$

$$x_{33} = 12$$

total cost

$$(18 \times 6) + (12 \times 9) + (10 \times 6) + (3 \times 13) + (12 \times 5) + (18 \times 4)$$

$$= 108 + 108 + 60 + 39 + 60 + 72$$

total cost $\boxed{447}$

least cost

6	8	7	1	18
9	6	13	12	25
17	8	5	4	30
30	10	15	18	73

6	8	7	1	18	18 0
9	6	13	12	25	15 0
17	8	5	4	30	15
30	10	15	18		
15	0	0	0		

Total cost

$$\begin{aligned}
 & (18 \times 1) + (15 \times 9) + (10 \times 6) + (15 \times 17) + \\
 & (15 \times 5) \\
 & = 18 + 135 + 60 + 255 + 75 \\
 & = 543.
 \end{aligned}$$

VAM Method

	6	8	7	1	18	I	II	III	IV
	9	6	13	12	25	5	-	-	-
	17	8	5	4	30	3	← 3	← 3	-
	30	10	15	18		1	1	1	1
	15								
I	3	2	2	3					
II	3	2	2	-					
III	3	-	2	-					
IV	11	-	2	-					

total cost

$$\begin{aligned} & (18 \times 1) + (15 \times 9) + (10 \times 6) + (15 \times 17) + (15 \times 5) \\ & = 18 + 135 + 60 + 255 + 75 \\ & = \boxed{543} \end{aligned}$$

7) Cost on team of Inventory Method.

Calculate EOQ :-

Annual Demand = ₹ 42,000 /-

Ordering cost = ₹ 300 per unit

Inventory carrying = 38%.

Solution:-

$$\begin{aligned} Q^* &= \sqrt{\frac{2AD}{h}} \\ &= \sqrt{\frac{2 \times 300 \times 42,000}{0.38}} \\ &= \sqrt{\frac{25,200,000}{0.38}} \\ &= \sqrt{66,315} \\ &= \boxed{8,1434} \end{aligned}$$

total cost

$$\begin{aligned} & \sqrt{2ADh} \\ &= \sqrt{2 \times 300 \times 42,000 \times 0.38} \\ &= \sqrt{9,576,000} \\ &= \boxed{3,094.51} \end{aligned}$$

8 What are the Operation Research of decision Making?

Decision Making:-

Decision literally means choosing from available alternatives the essential characteristics all decision are

(i) Trigger

(ii) Alternative at the disposal

(iii) Influencing factors.

Operation Research is the Science of Managing which is concerned with making decision most of the times

It is the decision science that helps the management to make better decisions is a pivotal word in Managing.

In OR scientific it used in order to make better management decision. The essential features of decision namely objectives, alternative and influencing factors or expressed.

in terms of scientific qualification
or mathematical solution.

9. $\max z = 3x_1 + 2x_2$

Subject to

$$5x_1 + x_2 \geq 10$$

$$x_1, x_2 \geq 6$$

$$x_1 + 4x_2 \geq 12$$

$$x_1, x_2 \geq 0$$

Solution:-

(i) $5x_1 + x_2 = 10$

$$x_1 = 0$$
$$0 + x_2 = 10$$
$$x_2 = 10$$

$$P(0, 10)$$

$$x_2 = 0$$
$$5x_1 + 0 = 10$$
$$x_1 = \frac{10}{5} = 2$$

$$P(2, 0)$$

(ii) $x_1, x_2 = 6$

$$x_1 = 0$$
$$0 + x_2 = 6$$
$$x_2 = 6$$

$$P(0, 6)$$

$$x_2 = 0$$
$$x_1 + 0 = 6$$
$$x_1 = 6$$

$$P(6, 0)$$

(iii) $x_1 + 4x_2 = 12$

$$x_1 = 0$$
$$0 + 4x_2 = 12$$

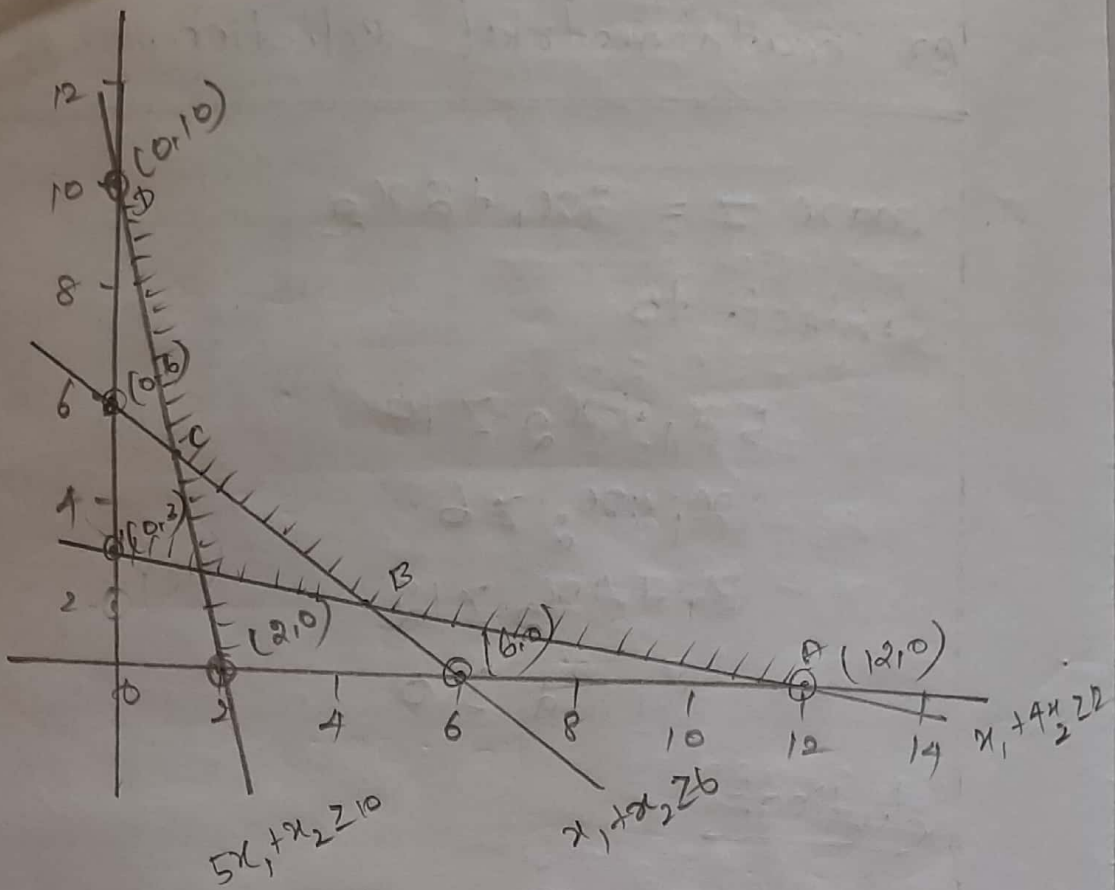
$$x_2 = \frac{12}{4}$$

$$x_2 = 3$$

$$P(0, 3)$$

$$x_2 = 0$$
$$x_1 + 0 = 12$$
$$x_1 = 12$$

$$P(12, 0)$$



$$A = (0, 10) = 20$$

$$B = (6, 0) = 24$$

$$C = (4, 2) = 16$$

$$D = (12, 0) = 36$$

$$B \quad x_1 + x_2 = 6 \quad \text{--- (1) } \times 5$$

$$5x_1 + x_2 = 10 \quad \text{--- (2) } \times$$

$$4x_2 = 20$$

$$x_2 = \frac{20}{4} = 5$$

$$x_1 = 1$$

$$C \quad x_1 + 4x_2 = 12 \quad \text{--- (1)}$$

$$x_1 + x_2 = 6 \quad \text{--- (2)}$$

$$x_1 + 4x_2 = 12$$

$$4x_1 + 4x_2 = 24$$

$$3x_1 = 12$$

$$3x_1 = 12$$

$$x_1 = \frac{12}{3} = 4$$

$$\boxed{x_1 = 4}$$

Substitued I

$$x_1 + 5x_1 = 6$$

$$x_1 + 5x_1 = 6$$

$$x_1 + 5 = 6$$

$$x_1 = 6 - 5$$

$$x_1 = 1$$

Substitued II

$$x_1 + x_2 = 6$$

$$4 + x_2 = 6$$

$$x_2 = 6 - 4$$

$$\boxed{x_2 = 2}$$

$$\begin{aligned} \text{A) } z &= 3x_1 + 2x_2 \\ &= 3 \times 0 + 2 \times 10 = z \\ 0 + 20 &= z \end{aligned}$$

$$\boxed{z = 20}$$

$$\text{C) } z = 3x_1 + 2x_2$$

$$3 \times 4 + 2 \times 2$$

$$12 + 4 = z$$

$$\boxed{z = 16}$$

$$\begin{aligned} \text{B) } z &= 3x_1 + 2x_2 \\ 3 \times 1 + 2 \times 5 &= z \\ 3 + 10 &= z \end{aligned}$$

$$\boxed{z = 13}$$

$$\begin{aligned} \text{D) } z &= 3x_1 + 2x_2 \\ 3 \times 12 + 2 \times 0 &= z \\ 36 + 0 &= z \end{aligned}$$

$$\boxed{z = 36}$$

10) Calculate NCWR, Least Minima, VAM Method:

8	7	5	9	25
4	8	6	5	20
16	7	18	4	50
15	10	50	20	95

$$a_{ij} = 95 = b_j$$

NCWR

<u>15</u>	<u>10</u>			25
8	7	<u>5</u>	9	10
4	8	<u>6</u>	5	20
16	7	<u>18</u>	<u>4</u>	50 20
15	10	50 30	20	

$$x_{11} = 15$$

$$x_{12} = 10$$

$$x_{23} = 6$$

$$x_{33} = 30$$

$$x_{34} = 20$$

total cost

$$(15 \times 8) + (10 \times 7) + (6 \times 20) + (18 \times 80) + (4 \times 20)$$

$$= 120 + 70 + 120 + 540 + 80$$

$$\text{total cost} = \boxed{930}$$

		25		
8	7	5	9	25 0
15		5		
A	8	6	5	20 5
	10	20	20	
16	7	18	4	50 20
15	10	50	20	
	0	25	20	
		20		

Total cost

$$\begin{aligned}
 & (25 \times 5) + (15 \times 4) + (5 \times 6) + (10 \times 7) \\
 & + (20 \times 18) + (20 \times 4) \\
 & = 125 + 60 + 30 + 70 + 360 + 80 \\
 & = \boxed{725}
 \end{aligned}$$

VAN

		25		25	2	2	2	2	-
8	7	5	9	25					
15		5		5	1	1	1	1	1
A	8	6	5	20					
	10	20	20	30 20					
16	7	18	4	50	3	3	11	2	2
15	10	50	20						
		25	20						
A	-	1	1						
-	-	1	1						
-	-	1	1						
-	-	12	-						

Total cost

$$(25 \times 5) + (15 \times 4) + (5 \times 6) + (10 \times 7) + (20 \times 18) + (20 \times 4)$$

$$= 125 + 60 + 30 + 70 + 360 + 80$$

$$\boxed{725}$$

11) Machine 61,000/-

Scrap value = 1000/-

year	1	2	3	4	5	6	7	8
M.C	1000	2500	4000	6000	9000	12000	16000	20000
year	2	2	4	5	6			
	Maintenance Cost	Cumulative	C-S	3+4	5/n			
1	1000	1000	60,000	61,000	61,000			
2	2500	3500	60,000	63,500	31,750			
3	4000	7500	60,000	67,500	22,500			
4	6000	13500	60,000	73,500	18,375			
5	9000	22500	60,000	82,500	16500			
6	12000	34500	60,000	94500	15750			
7	16000	50500	60,000	1,10,500	15785.7			
8	20000	52500	60,000	1,12,500	14,062.5			

Solution:-

It may be minimum total average cost 1406 during 8th year. Therefore the Machine should be replaced after every 8th year otherwise the average cost per year would start increasing.

- 12) Use & Limitations of Operation Research
- * It provides a logical and systematic approach to the problem
 - * It allows modification of Mathematical Solution before they are put to use
 - * It suggests all the alternative source of action for the same Management
 - * It helps in finding avenues for new research and improvement in the system.
 - * It specifies impute Quality of decision.
 - * It indicates the scope as well as limitation of a problem.

Limitation of Operation Research:-

(i) Models are the only idealized representations of reality and cannot be regarded as absolute in any case

(ii) The validity of the model of a particular situation can be ascertained only by conducting experiments.

13. A Machine Cost ₹ 10,000/- Operating Cost & Resale values are given below:-

Year	1	2	3	4	5	6	7	8
Operating Cost	1000	1200	1400	1700	2000	2500	3000	3500
Resale Value	6000	4000	3800	2600	2500	2400	2000	1600

Year	$f(n)$	$\Sigma f(n)$ Cumulative	S	$C-S$	$TC =$ $3+5$ 6	b/n
1	2	3	4	5	6	7
1	1000	1000	6000	4000	5000	5000
2	1200	2200	4000	6000	6200	4100
3	1400	3600	3200	6800	10400	3466.6
4	1700	5300	2600	7400	12700	3175
5	2000	7300	2500	7500	14800	2960
6	2500	9800	2400	7600	17400	<u>2900</u>
7	3000	12800	2000	8000	20800	2971.4
8	3500	16300	1600	9400	25700	3212.5

Solution:-

It may be minimum total average cost 2900 during 6th year therefore the Machine should be replace after every 6th year otherwise the average cost per year would start increasing.