

I BSC (CS, IT)

And

BCA

Operation Research

2 Mark

1. State the mathematical formulation of LPP.
2. State the Canonical form of LPP
3. Define graphical solution form of LPP
4. Define feasible solution
5. Express the following LPP into standard form.
$$\text{Max } Z = 4x_1 + 2x_2 + 6x_3$$

Sub to constraint

$$2x_1 + 3x_2 + 2x_3 \geq 6$$
$$3x_1 + 4x_2 \geq 8$$
$$6x_1 - 4x_2 + x_3 \leq 10, \quad x_1, x_2, x_3 \geq 0$$
6. Define standard form
7. Express the following LPP into canonical form.
$$\text{Max } Z = 2x_1 + 3x_2 + x_3$$

Sub to constraint

$$4x_1 + 3x_2 + x_3 \leq 6$$
$$x_1 + 5x_3 - 7x_4 \geq 4$$

and $x_1, x_2, x_3 \geq 0$ and x_2 is unrestricted.
8. Define characteristics of the Canonical form
9. Define slack
10. Define Surplus
11. What is artificial variable
12. Define Big-M method
13. Write any one condition for big-M method
14. Define simplex method of LPP
15. Discuss the north west corner rule
16. What is transportation problem
17. What is types of transportation problem and give Example for types
18. How many methods in transportation problem
19. What is the initial basic feasible solution
20. What is unbalanced problem

- 21. Define Sequencing problem
- 22. Define total elapsed time (T)
- 23. Define idle time
- 24. Define Graphical method
- 25. Define processing of n jobs 2 machine
- 26. Define processing of n jobs 3 machine
- 27. Define network
- 28. Define PERT
- 29. Define critical path
- 30. Define independent float
- 31. Define fulkerson's rule
- 32. what is the difference between PERT and CPM
- 33. Define term project planning?
- 34. what is dummy activity?
- 35. what is Assignment problem

5 marks

1. Express the following LPP into canonical form

$$\text{Max } Z = 2x_1 + 3x_2 + x_3$$

sub to constraint

$$4x_1 - 3x_2 + x_3 \leq 6$$

$$x_1 + 5x_2 - 7x_3 \geq -4$$

$x_1, x_2, x_3 \geq 0$ and x_2 is unrestricted

2. using Graphical method

$$\text{Max } Z = 4x_1 + 3x_2$$

sub to constant

$$x_1 - x_2 \leq -1$$

$$-x_1 + x_2 \geq 0$$

$x_1, x_2 \geq 0$

3. Express the following LPP to Canonical form and Standard form

$$\text{Max } z = 2x_1 + 3x_2 + x_3$$

Sub to Constraint

$$4x_1 - 3x_2 + x_3 \leq 6$$

$$x_1 + 5x_2 - x_3 \geq -4$$

$$x_1, x_2, x_3 \geq 0$$

4. Explain the Role of Computer in OR

5. Explain the Procedure in mathematical formulation of LPP.

6. Explain the procedure in Graphical method.

7. Solve the following LPP by penalty method

$$\text{Max } z = 3x_1 + 2x_2$$

Sub to Constraint

$$2x_1 + x_2 \leq 2$$

$$3x_1 + 4x_2 \geq 12$$

$$\text{and } x_1, x_2 \geq 0$$

8. Solve the following LPP by using big-M method,

$$\text{Min } z = 4x_1 + 3x_2$$

subject to constraints

$$2x_1 + x_2 \geq 10$$

$$-3x_1 + 2x_2 \leq 6$$

$$x_1 + x_2 \geq 6$$

$$\text{and } x_1, x_2 \geq 0$$

9. write down the algorithm for big-M method

10. write down the algorithm for simplex method

11. Max $z = 3x_1 + 2x_2 + 5x_3$, find using simplex method subject to constraint

$$x_1 + 4x_2 \leq 420$$

$$3x_1 + 2x_3 \leq 460$$

$$x_1 + 2x_2 + x_3 \leq 430 \text{ and } x_1, x_2, x_3 \geq 0$$

12. Find using Char's method (or) Penalty method following LPP by Max $Z = 3x_1 + 2x_2$ sub to constraint

$$2x_1 + x_2 \leq 2$$

$$3x_1 + 4x_2 \geq 12 \text{ and } x_1, x_2 \geq 0$$

13. Find the non-negative value of simplex method

$$\text{Max } Z = 5x_1 + 3x_2$$

Subject to Constraints

$$x_1 + x_2 \leq 2$$

$$5x_1 + 2x_2 \leq 10$$

$$3x_1 + 8x_2 \leq 12 \text{ and } x_1, x_2 \geq 0$$

14. Find the initial basic feasible solution of the following transport problem by Northwest corner cell method

Source	Destination				Supply
	A	B	C	D	
I	3	1	7	4	250
II	2	6	5	9	350
III	8	3	3	2	400
	Demand	200	300	300	150

15. Find the initial basic feasible solution of the following transportation problem by Least cost method

Source	Destination				Supply
	S1	S2	S3	S4	
F1	4	6	8	8	40
F2	6	8	6	7	60
F3	5	7	6	8	50
	DEMAND	20	30	50	50

16. Find the initial basic feasible solution of the following transport problem in unbalanced problem by Least Cost method

Source	Destination			Supply
	I	II	III	
A	2	3	4	10
B	5	7	9	30
C	10	2	5	60
	Demand	20	25	45

17. Find the transportation using VAM

	Destination				Supply
	A	B	C	D	
I	3	1	7	4	300
II	2	6	5	9	400
III	8	3	3	2	500
Demand	250	350	400	200	

18. Find minimum job assignment for given problem

	J ₁	J ₂	J ₃	J ₄
P ₁	10	3	8	9
P ₂	7	5	4	8
P ₃	6	9	2	9
P ₄	8	7	10	9

19. Write down the algorithm for northwest corner method

20. write down the algorithm for least cost corner method

21. write down the algorithm of sequencing problem

22. There are two jobs to be processed through the 4 machines A, B, C and D through the processed time in hour

Job 1 A C B D
Job 2 D B A C are given as follows

		Machine			
	Jobs	A	B	C	D
Jobs	1	2	4	5	1
	2	6	4	2	3

23. Find the sequence that minimize the total elapsed time required to complete the following jobs on 3 machines in order A B C

Jobs	I	II	III	IV	V
M ₁ (A)	8	10	6	7	11
M ₂ (B)	5	6	2	3	4
M ₃ (C)	4	9	8	6	5

24.

Find n Jobs on machines

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Jobs	A	B	C	D	E
M ₁	10	12	8	15	16
M ₂	3	2	4	1	5
M ₃	5	6	4	7	3
M ₄	14	7	12	8	10

25. write down the steps for n Jobs on 2 machines

26. Explain the estimate time in PERT

27. A Project consists of 7 activities given below

Activity	A	B	C	D	E	F	G
Preceding Activity	-	-	-	A, B	A, B	C, E	C, D, E
Duration (days)	4	7	6	5	7	6	5

draw the network and find the Project length, Completion time and calculate the total float for each activity.

28. The following table indicates the details of a Project that the determine are in days 'a' refer a optimistic time refers to most likely time 'b' refers to pessimistic time duration.

Activity	1-2	1-3	1-4	2-4	2-5	3-5	4-5
a	2	3	4	8	6	2	2
m	4	4	5	9	8	3	5
b	5	6	6	11	12	4	7

Draw the network and find critical path and expected standard deviation of completion time.

29. Explain Fulkerson's rule

30. calculate the earliest start and finish time and total start and finish time of each activity of the Project given below

Activity	1-2	1-3	2-4	3-4	3-6	4-9	5-6	5-7	6-8	7-8
Duration	4	1	1	1	6	5	4	8	1	2

1. A firm manufacture two types of product A and B and sell them out at a profit of rupees 2 on type A and profit of Rs 3 on type B. Each product processed on two machine M₁ and M₂. Type A require one minute of processing time on M₁ and two minute on M₂. Type B requires one minute on M₁ and one minute on M₂. The machine M₁ is available are not more than six hours 40 minutes with machine m₂ is available for 10 hrs during any working day formulate the problem as LPP & as to maximize the profit

2. using Graphical method

$$\text{Max } z = 2x_1 + 3x_2$$
 Subject to constraint

$$x_1 - x_2 \leq 2$$

$$x_1 + x_2 \geq 4 \text{ and } x_1, x_2 \geq 0.$$

3. solve the following LPP by graphical method

$$\text{Max } z \geq 3x_1 + 2x_2$$
 Subject to constraint

$$-2x_1 + x_2 \leq 1$$

$$x_2 \leq 2$$

$$x_1 + x_2 \leq 3 \text{ and } x_1, x_2 \geq 0$$

4. Three products this products are processed on three different machines time required to manufacture unit of each unit of three products and daily capacity on given table.

machine	Time per unit			machine Capacity
	P	P	P	
M ₁	2	3	2	440
M ₂	4	-	3	470
M ₃	2	5	-	430

It is required to determine the number of units to be manufactured for each product the profit per unit for product 1, 2, 3, 4 and 6 respectively it is measured that all the among produced are consumed in the market formulated the mathematical model for the Problems.

5. a firm Produces is having the following specific gravity ≤ 0.98 , Chromium $\geq 8\%$, melting point $\geq 450^\circ\text{C}$. Raw material a, b and c have the properties showing the table can be used

Property	Raw material		
	A	B	C
Specific gravity	0.92	0.97	1.04
Chromium	7%	13%	16%
Melting Point	440°C	490°C	480°C

Cost of various raw materials per unit can be Rs 90 for A, Rs 280 for B and Rs 40 for C. Find the properties in which A, B and C used to obtain an alloy of desired properties which the cost of value material is minimum.

6. Solve two phase simplex method to use $Max z = 5x_1 + 8x_2$ subject to constraints $3x_1 + 2x_2 \geq 3$
 $x_1 + 4x_2 \geq 4$
 $x_1 + x_2 \leq 5$ and $x_1, x_2 \geq 0$.

7. Solve the following LPP using simplex method
 $Max z = 4x_1 + 10x_2$
 subject to constraints
 $2x_1 + x_2 \leq 50$
 $2x_1 + 5x_2 \leq 100$
 $2x_1 + 3x_2 \leq 90$ and $x_1, x_2 \geq 0$.

8. Explain briefly about two phase duality method

9. Solve the following LPP using Simplex method
 $Max z = x_1 + 3x_2 + 6x_3$
 subject to constraints
 $x_1 + 5x_2 \leq 300$
 $3x_1 + 2x_3 \leq 250$
 $x_1 + 2x_2 + x_3 \leq 320$ and $x_1, x_2, x_3 \geq 0$.

10. Write algorithm about channels method

11. Six machines & 5 jobs processing cost is given in table. make an assignment problem and find out optimal cost (minimization)

	J ₁	J ₂	J ₃	J ₄	J ₅
M ₁	6	2	5	2	6
M ₂	2	5	8	7	7
M ₃	7	8	6	9	8
M ₄	6	2	3	4	5
M ₅	9	3	8	9	7
M ₆	4	7	4	6	8

11. Find the initial basic feasible solution of the following transportation problem using VAM method and then optimize the situation using UV method.

	A	B	C	D	Supply
I	3	1	7	4	250
II	2	6	5	9	350
III	8	3	3	2	400
Demand	200	300	350	150	

12. write the algorithm of VAM method
 13. write the algorithm of Assignment problem.
 14. Find the initial basic feasible solution of following transportation problem using Northwest and least cost method

	A	B	C	D	Supply
I	5	2	4	3	22
II	4	8	1	6	15
III	4	6	7	5	8
Demand	7	12	17	9	

15. Solve using assignment problem for 5 jobs to 5 machine

	A	B	C	D	E
I	5	11	10	12	4
II	2	4	6	3	5
III	3	12	5	14	6
IV	5	14	4	11	7
V	7	7	8	12	5

16. write down the steps for n jobs m machines and also Two jobs on n machines
 17. Define no passing rule in a sequencing problem.
 18. Find n jobs m machine.

machine/jobs	A	B	C	D
M1	18	17	11	20
M2	8	6	5	4
M3	7	9	8	8
M4	2	6	5	4
M5	10	8	7	3
M6	25	19	15	12

19. What is a graphical method? How to using two jobs on n machines.

20. Two jobs have to be processed through each of the machines the processing time on each machine and sequence of jobs

Job 1. $A \rightarrow C \rightarrow D \rightarrow B \rightarrow E \rightarrow F$

Job 2. $A \rightarrow C \rightarrow B \rightarrow D \rightarrow F \rightarrow E$

	Machine					
	A	B	C	D	E	F
Job 1	20	30	10	10	25	15
Job 2	10	15	30	10	20	15

In which order should jobs be done on each of the machine to maximize the total time to process the jobs? find the minimum elapsed time.

21. calculate the total float, free float and independent float for the project whose activity for given below

Activity	1-2	1-3	1-5	2-3	2-4	3-4	3-5	3-6	4-6	5-6
Duration (in weeks)	8	7	12	4	10	3	5	10	7	4

22. Construct the network for the project whose the activity and three times estimates of the activities (in weeks) are given below.

- i) Expect the duration of the each activity
- ii) Expect the variance of each activity
- iii) Expect the variance of the project length

Activity	1-2	2-3	2-4	3-5	4-5	4-6	5-7	6-7	7-8	7-9	8-10	9-10
t_o	3	1	2	3	1	3	4	6	2	1	4	3
t_m	4	2	3	4	3	5	5	7	4	2	6	5
t_p	5	3	4	5	5	7	6	8	6	3	8	7

23. A small project is composed of activities of given below

Activity	1-2	1-3	1-4	2-5	3-5	4-6	5-6
t_o	1	1	2	1	2	2	3
t_m	1	4	2	1	5	5	6
t_p	7	7	8	1	14	8	15

- i) Draw the network
- ii) find the critical path
- iii) Determine the expected standard deviation of the completion time

24. The data for a small PERT project is as given below

(11)

A	B	C	D	E	F	G	H	I	J	K
3	2	6	2	5	3	3	1	4	1	2
6	5	12	5	11	6	9	4	19	2	4
15	14	30	8	17	15	27	7	28	9	12

Procedure relationship A, B, C can start immediately

$A < D, I$; $B < G, F$; $D < G, F$; $C < E$; $E < H, K$;

$F < H, K$; $G, H < J$

- i) Draw the project network
- ii) calculate the earliest and latest expected time to reach node and find critical path
- iii) Also find expected variance of the project length

25. A project has 9 activities, the expected time of each activity as follows.

Activity	1-2	1-3	2-4	3-4	4-6	5-6	3-5	5-7	6-7
Days	6	8	7	12	3	5	7	11	10

- i) Draw the project work
- ii) Identify the critical path
- iii) Find the project duration
- iv) What is the slack at each activity?